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Whole Earth Telescope observations of the subdwarf B star KPD 1930+2752: a rich, short-period pulsator in a close binary

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ABSTRACT

KPD 1930+2752 is a short-period pulsating subdwarf B (sdB) star. It is also an ellipsoidal variable with a known binary period of 2.3 h. The companion is most likely a white dwarf and the total mass of the system is close to the Chandrasekhar limit. In this paper, we report the results of Whole Earth Telescope (WET) photometric observations during 2003 and a smaller multisite campaign of 2002. From 355 h of WET data, we detect 68 pulsation frequencies and suggest an additional 13 frequencies within a crowded and complex temporal spectrum between 3065 and 6343 μHz (periods between 326 and 157 s). We examine pulsation properties including phase and amplitude stability in an attempt to understand the nature of the pulsation mechanism. We examine a stochastic mechanism by comparing amplitude variations with simulated stochastic data. We also use the binary nature of KPD 1930+2752 for identifying pulsation modes via multiplet structure and a tidally induced pulsation geometry. Our results indicate a complicated pulsation structure that includes short-period (≈ 16 h) amplitude variability, rotationally split modes, tidally induced modes and some pulsations which are geometrically limited on the sdB star.

Key words: binaries: close – stars: general – stars: oscillations – subdwarfs – oscillations: individual: KPD 1930+2752.

1 INTRODUCTION

Subdwarf B (sdB) stars are thought to have masses of about $0.5 M_{\odot}$ with thin ($< 10^{-2} M_{\odot}$) hydrogen shells and temperatures from 22 000 to 40 000 K (Heber et al. 1984; Saffer et al. 1994). Shell hydrogen burning cannot be supported by such thin envelopes, and it is likely that they proceed directly to the white dwarf cooling track without reaching the asymptotic giant branch (Saffer et al. 1994).

Pulsating sdB stars with periods of a few minutes (officially V361 Hya, and also known as EC 14026 or sdBV stars) were first observed by Kilkenney et al. (1997), nearly simultaneous to their predicted existence by Charpinet et al. (1996, 1997). The sdBV stars have pulsation periods ranging from 90 to 600 s with amplitudes typically near or below 1 per cent. The pulsations are likely p modes driven by the κ mechanism due to a diffusive iron-group opacity bump in the envelope (Charpinet et al. 1997; Jeffery & Saio 2007). Subdwarf B pulsators are typically found among the hotter sdB stars, with $T_{\text{eff}} \approx 34\,000$ K and $\log g \approx 5.8$. Reviews of this pulsation class include an observational review by Reed et al. (2007a) for an of 23 resolved class members and by Charpinet, Fontaine & Brassard (2001) who described the pulsation mechanism. Another class of pulsating sdB stars have periods longer than 45 min, are likely g-mode pulsations and are designated V1093 Her, but commonly known as PG 1716 stars (Green et al. 2003; Reed et al. 2004a). General reviews of sdB stars and pulsators are of Heber (2009) and Østensen (2009). Our target is a p-mode, sdBV-type pulsator.

KPD 1930+2752 (also V2214 Cyg and hereafter KPD 1930) was discovered to be a variable by Billères et al. (2000, hereafter B00), who obtained data during four nights within one week. Their longest run was 5 h, yet within this limited data set, they detected 45 separate frequencies, which indicate that KPD 1930 is an interesting and complex pulsator. A velocity study confirmed the $2^{\text{h}}17^{\text{m}}$ binary period and, using the canonical sdB mass of $0.5 M_{\odot}$, determined the

companion mass to be $0.97 \pm 0.01 M_{\odot}$ (Maxted, Marsh & North 2000). As the companion is not observed either photometrically or spectroscopically, it is likely a white dwarf, placing the mass of the system over the Chandrasekhar limit. A study by Ergma, Fedorova & Yungelson (2001) suggested that the binary will shed sufficient mass to avoid a Type Ia supernova and will merge to form a massive white dwarf. With a rich, unresolved pulsation spectrum and the opportunity to learn some very interesting physics via asteroseismology, KPD 1930 was chosen for observation by the Whole Earth Telescope (WET). KPD 1930 also has an infrared companion ≈ 0.5 arcsec away (Østensen, Heber & Maxted 2005).

2 OBSERVATIONS

KPD 1930 was the target of the WET run Xcov 23. Nearly 355 h of data were collected at 17 observatories from 2003 August 15 to September 9. The individual runs are provided in Table 1. Overall, these data have an observational duty cycle of 36 per cent which is less than typical WET campaigns. Because of the crowded field, most of the data were obtained with CCD photometers whereas some were obtained with photoelectric (photomultiplier tube) photometers. The photoelectric data were reduced in the usual manner as described by Kleinman, Nather & Phillips (1996). The standard procedures of CCD image reduction, including bias subtraction, dark correction and flat-field correction, were followed using IRAF packages. Differential intensities were determined via aperture photometry with the aperture optimized for each individual run with varying numbers of comparison stars depending on the field of view. Lightcurves are shown in Fig. 1.

We will also examine a small multisite campaign that obtained data during 2002 July. In total, almost 45 h of data were obtained from McDonald (the 2.1-m Otto Struve Telescope), San

Table 1. WET observations of KPD 1930+2752 during XCOV23 in 2003.

Run	Length (h)	Date UT	Observatory	Run	Length (h)	Date UT	Observatory
t081403	5.5	Aug. 15	Mt Cuba 0.4 m	loi2708	3.0	Aug. 27	Loiano 1.5 m
phot081503	6.4	Aug. 16	Mt Cuba 0.4 m	gv30808	5.8	Aug. 27	OHP 1.9 m
phot081703	0.7	Aug. 18	Mt Cuba 0.4 m	a0688	2.0	Aug. 28	McDonald 2.1 m
hunaug18	3.1	Aug. 18	Piszkesteto 1.0 m	mdr245	0.9	Aug. 28	KPNO 2.1 m
NOT_Aug19	7.8	Aug. 19	NOT 2.6 m	haw28aug	3.0	Aug. 28	Hawaii 0.6 m
phot081903	6.5	Aug. 19	Mt Cuba 0.4 m	lulin28aug	7.5	Aug. 28	Lulin 1.0 m
hunaug19	4.3	Aug. 19	Piszkesteto 1.0 m	turkaug28	2.5	Aug. 28	Turkey 1.5 m
NOT_Aug20	8.6	Aug. 20	NOT 2.6 m	jr0828	3.7	Aug. 28	Moletai 1.65 m
lna20aug	4.4	Aug. 20	LNA 0.6 m	retha-0031	3.4	Aug. 28	SAAO 1.9 m
phot082003	6.9	Aug. 20	Mt Cuba 0.4 m	phot082903	4.9	Aug. 29	Mt Cuba
hunaug20	4.6	Aug. 20	Piszkesteto 1.0 m	a0690	0.2	Aug. 29	McDonald 2.1 m
hunaug21	4.8	Aug. 21	Piszkesteto 1.0 m	mdr246	3.8	Aug. 29	KPNO 2.1 m
NOT_Aug21	8.8	Aug. 21	NOT 2.6 m	haw29aug	3.0	Aug. 29	Hawaii 0.6 m
lna21aug	4.5	Aug. 21	LNA 0.6 m	turkaug29	5.5	Aug. 29	Turkey 1.5 m
lulin21aug	7.0	Aug. 21	Lulin 1.0 m	retha-0041	3.9	Aug. 29	SAAO 1.9 m
NOT_Aug22	8.7	Aug. 22	NOT 2.6 m	gv30809	5.7	Aug. 29	OHP 1.9 m
lna22aug	1.3	Aug. 22	LNA 0.6 m	mdr247	6.8	Aug. 30	KPNO 2.1 m
haw22aug	1.0	Aug. 22	Hawaii 0.6 m	haw30aug	2.4	Aug. 30	Hawaii 0.6 m
lulin22aug	2.4	Aug. 22	Lulin 1.0 m	turkaug30	4.3	Aug. 30	Turkey 1.5 m
suh-114	3.9	Aug. 22	Suhora 0.6 m	retha-0051	3.9	Aug. 30	SAAO 1.9 m
gv30801	2.5	Aug. 22	OHP 1.9 m	loi0830	0.1	Aug. 30	Loiano 1.5 m
NOT_Aug23	6.5	Aug. 23	NOT 2.6 m	mdr248	6.5	Aug. 31	KPNO 2.1 m
lna23aug	3.1	Aug. 23	LNA 0.6 m	haw31aug	2.9	Aug. 31	Hawaii 0.6 m
haw23aug	3.6	Aug. 23	Hawaii 0.6 m	turkaug31	5.5	Aug. 31	Turkey 1.5 m
lulin23aug	6.8	Aug. 23	Lulin 1.0 m	se0103q1	2.6	Sep. 01	SSO 1.0 m
gv30803	1.1	Aug. 23	OHP 1.9 m	turkse01	5.0	Sep. 01	Turkey 1.5 m
lna24aug	4.8	Aug. 24	LNA 0.6 m	mdr249	3.6	Sep. 02	KPNO 2.1 m
phot082403	6.9	Aug. 24	Mt Cuba 0.4 m	se0203q1	4.6	Sep. 02	SSO 1.0 m
haw24aug	0.5	Aug. 24	Hawaii 0.6 m	turkse02	4.9	Sep. 02	Turkey 1.5 m
gv30805	3.5	Aug. 24	OHP 1.9 m	haw03sep	2.3	Sep. 03	Hawaii 0.6 m
phot082503	3.8	Aug. 25	Mt Cuba 0.4 m	se0303q1	4.5	Sep. 03	SSO 1.0 m
haw25aug	0.7	Aug. 25	Hawaii 0.6 m	wise03sep	6.0	Sep. 03	Wise 1.0 m
lulin25aug	0.2	Aug. 25	Lulin 1.0 m	haw04sep	2.4	Sep. 04	Hawaii 0.6 m
suh-116	3.1	Aug. 25	Suhora 0.6 m	se0403q1	4.6	Sep. 04	SSO 1.0 m
gv30806	4.5	Aug. 25	OHP 1.9 m	wise04sep	3.8	Sep. 04	Wise 1.0 m
phot082603	6.6	Aug. 26	Mt Cuba 0.4 m	hunsep04	1.7	Sep. 04	Piszkesteto 1.0 m
a0684	0.5	Aug. 26	McDonald 2.1 m	haw05sep	2.5	Sep. 05	Hawaii 0.6 m
a0685	0.3	Aug. 26	McDonald 2.1 m	wise05sep	7.0	Sep. 05	Wise 1.0 m
lulin26aug	7.0	Aug. 26	Lulin 1.0 m	haw06sep	2.2	Sep. 06	Hawaii 0.6 m
retha-0020	0.7	Aug. 26	SAAO 1.9 m	wise06sep	7.0	Sep. 06	Wise 1.0 m
gv30807	4.9	Aug. 26	OHP 1.9 m	hunsep06	4.8	Sep. 06	Piszkesteto 1.0 m
lna27aug	3.5	Aug. 27	LNA 0.6 m	haw07sep	1.2	Sep. 07	Hawaii 0.6 m
lulin27aug	7.4	Aug. 27	Lulin 1.0 m	hunsep07	4.6	Sep. 07	Piszkesteto 1.0 m
retha-0021	3.7	Aug. 27	SAAO 1.9 m	hunsep09	0.7	Sep. 09	Piszkesteto 1.0 m

Table 2. Observations of KPD 1930+2752 during 2002.

Run	Length (h)	Date UT	Observatory	Run	Length (h)	Date UT	Observatory
20710	3.5	July 10	Suhora 0.6 m	A0302	4.0	July 14	McDonald 2.1 m
20711	1.8	July 11	Suhora 0.6 m	A0304	3.9	July 15	Suhora 0.6 m
A0296	2.0	July 11	McDonald 2.1 m	20717	5.9	July 15	McDonald 2.1 m
20712	5.3	July 12	Suhora 0.6 m	sp1	2.4	July 17	Suhora 0.6 m
A0300	0.3	July 13	McDonald 2.1 m	20720	2.2	July 17	S.P. Martir 1.5 m
A0301	4.5	July 13	McDonald 2.1 m	sp2	2.4	July 20	Suhora 0.6 m
20714	1.4	July 14	Suhora 0.6 m	20715	4.2	July 20	S.P. Martir 1.5 m

Pedro-Martir (1.5 m) and Suhora (0.6 m) observatories. Specifics of these runs are given in Table 2.

As sdB stars are substantially hotter than typical field stars, differential light curves are not flat due to atmospheric reddening. A

low-order polynomial was fitted to remove nightly trends from the data. Finally, the light curves were normalized by their average flux and centred around zero, so the reported differential intensities are $\Delta I = (I/\langle I \rangle) - 1$. Amplitudes are given as milli-modulation

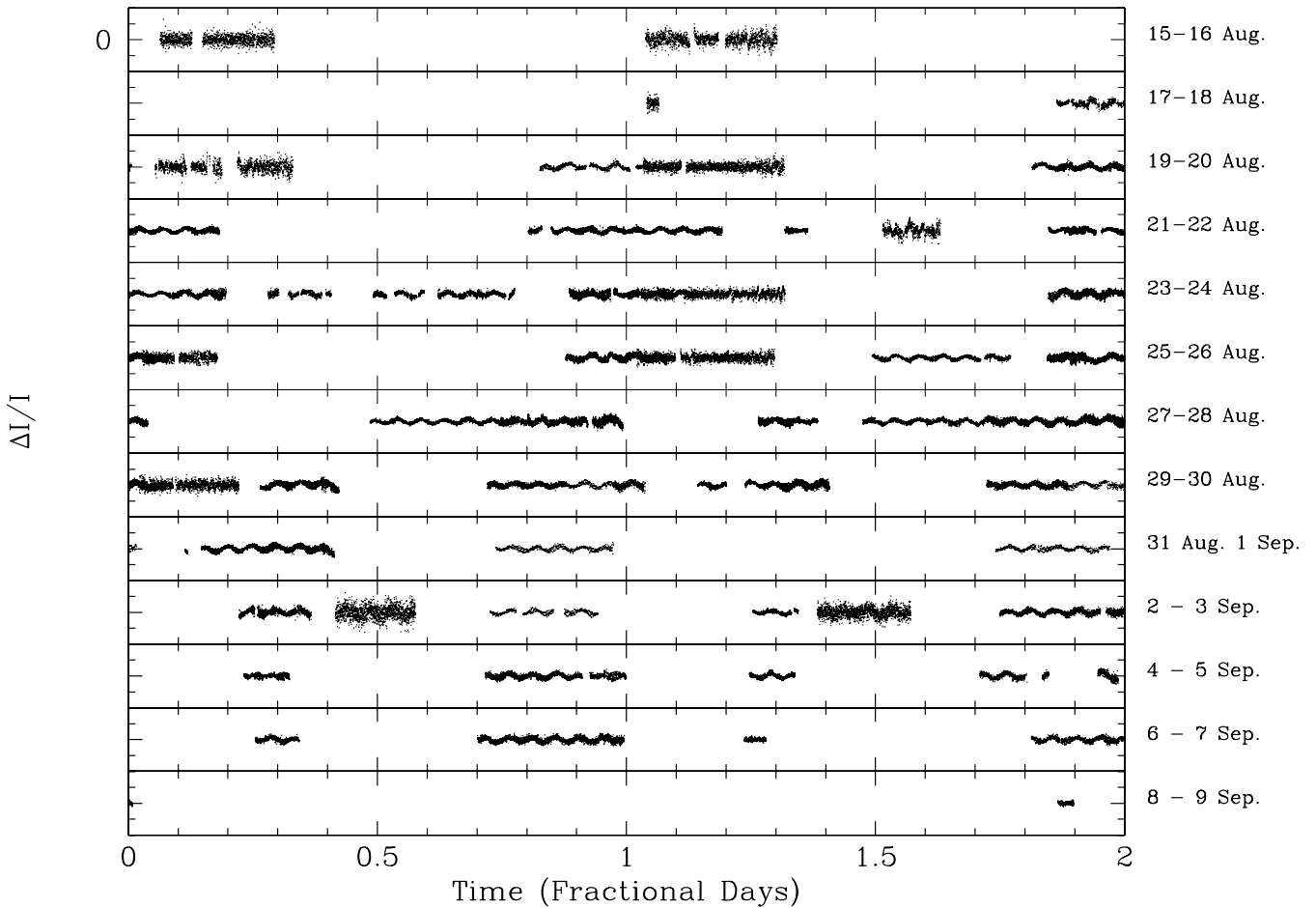


Figure 1. Light curves showing all data obtained during Xcov 23. Each panel is 2 d with the dates given on the right-hand side.

amplitudes (mma), with 10 mma corresponding to 1.0 per cent or 9.2 mmag.

3 ANALYSIS

3.1 Orbital parameters

The largest variation in the light curve is caused by an ellipsoidal variation of the sdB star. In removing this variation to examine the pulsations, we can deduce some of the orbital properties. We defer attempting a complete binary solution to a work in progress (Pablo et al., private communication), but provide some basic information here that is obvious from the data. Non-linear least-squares (NLLS) fitting to the data (2002 and 2004) provides a frequency of ellipsoidal variation of $243.369\,87 \pm 0.000\,07\,\mu\text{Hz}$. The binary period is twice that at $8217.994 \pm 0.002\,\text{s}$ or $0.095\,115\,67 \pm 0.000\,000\,03\,\text{d}$. Our value is within that found by B00 but outside the errors of the period determined by Geier et al. (2007, hereafter G07). G07 had 2900 spectroscopic data points unevenly scattered throughout 4 yr while we had 36 per cent coverage during 26 d in 2003 and $\sim 45\,\text{h}$ spanning 7 d in 2002. As the epochs of our data overlap, period change can be ruled out and it is most likely that one (or both) of us is underestimating our errors. Fig. 2 shows modified Xcov 23 data folded over the binary period. The pulsations make the light curve very broad and it even appears that a pulsation frequency is an integer multiple of the binary period. However that is not the case, but rather that there are many pulsation frequencies between 33 and 34

times the orbital frequency (see Section 3.2). To transform the broad pulsation-included light curve into a narrower, pre-whitened form, we used our best data (Group II), pre-whitened by all 61 pulsation frequencies. Then we phase-folded the data over the orbital period, did a 60-point ($\approx 11.5\,\text{s}$) smoothing and fitted an additional three frequencies. We then pre-whitened these three frequencies from the original, non-phase-folded data, phase folded again and smoothed by 60 ($\approx 11.5\,\text{s}$), 168 ($\approx 30\,\text{s}$) and 335 ($\approx 60\,\text{s}$) points. The differently smoothed data did not affect the maxima and minima of the orbital variations, and so we used the 335-point smoothed data, shown as a solid line in Fig. 2, to examine the ellipsoidal variations.

Using radial velocity data, G07 estimate the orbital inclination as $i \sim 80^\circ$. At this inclination, the white dwarf companion should eclipse the sdB star. An eclipse is shown for $i = 80^\circ$ in fig. 8 of G07 and using the orbital parameters of G07, we produced a simulated light curve with BINARY MAKER 3 (Fig. 3).¹ Our simulation was not intended to fit the actual data, but rather to illustrate the eclipse shape. From the simulation, the eclipse duration would be $\approx 164\,\text{s}$ or nearly three of our binned data points (at a binning of 335 points) with a depth of 0.2 per cent. While the observed minima are uneven, the shape and depth do not match those of an eclipse. We can therefore rule out inclinations for which an eclipse should occur, namely $i \geq 78.5^\circ$, based on G07. The uneven minima indicate what would

¹ See www.binarymaker.com.

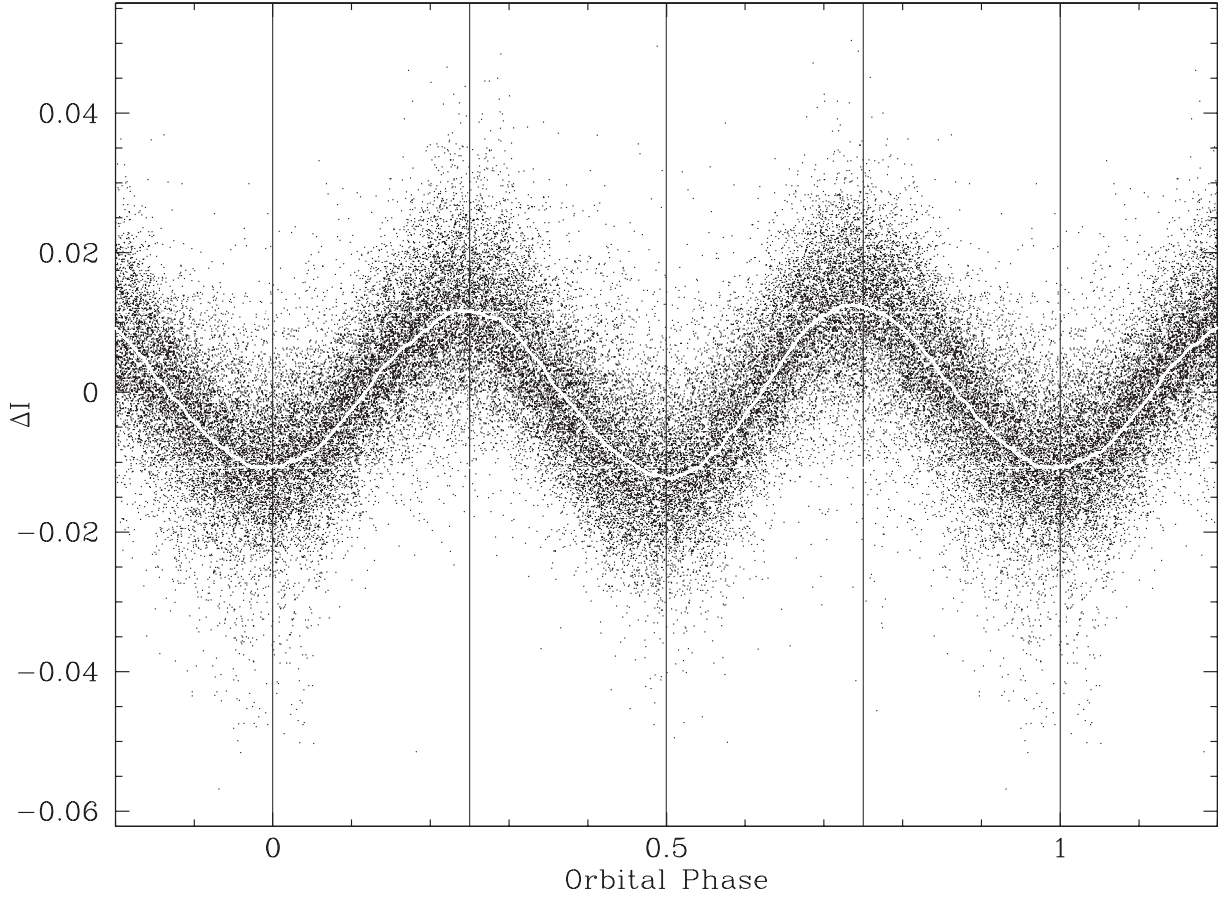


Figure 2. X-Cov 23 data folded over the binary period. The solid line is a result of pre-whitening the data and smoothing over 335 points (60 s in time) and the dashed horizontal lines indicate one maximum and minimum. For clarity, slightly more than one orbit is shown.

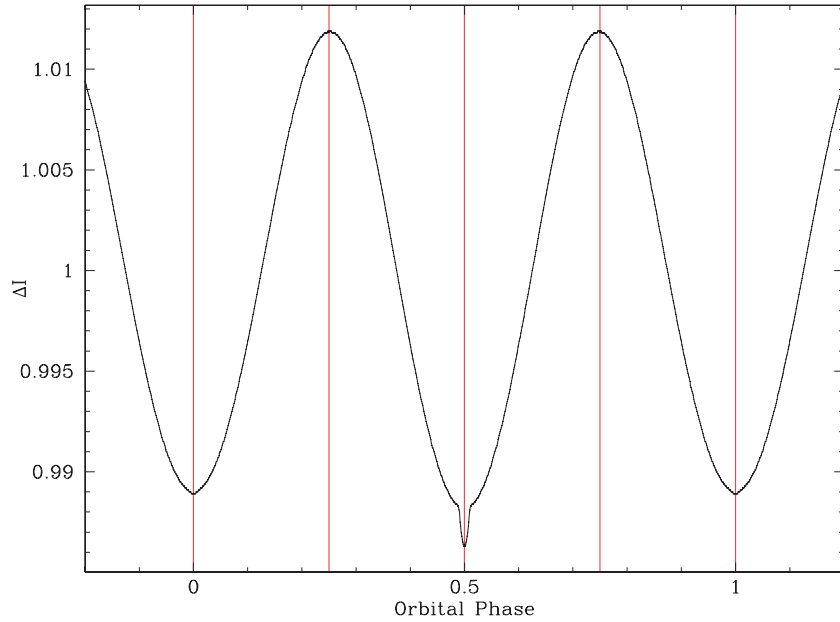


Figure 3. Simulated data showing the eclipse shape for $i = 80^\circ$.

be expected based on the tidal distortion (gravity darkening). The gravity of the white dwarf makes the sdB star slightly egg-shaped. When the marginally sharper end faces us, the line-of-sight angle does not go as deep at one optical depth as it does when the blunter

end faces us. This produces a fainter minimum when the sdB is farthest from us, and we view the slightly sharper end. A vastly exaggerated schematic of this is shown in Fig. 4 (a reconstructed image based on fig. 2 of Veen, van Genderen & van der Hucht

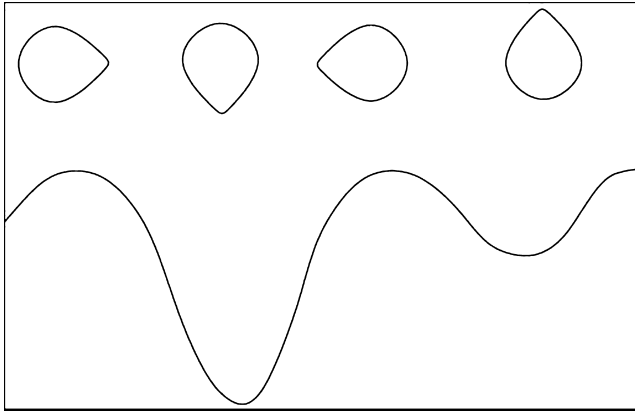


Figure 4. Exaggerated simulated data showing how limb darkening, combined with ellipsoidal variation, causes uneven minima.

2002). We fitted regions spanning 0.2 in phase with Gaussians to determine each maximum and minimum. The minimum at $\phi = 0.5$ is 0.18 ± 0.03 per cent fainter than the other minimum and using detailed models, this information, along with the amplitude of the ellipsoidal variation, should be sufficient to constrain the shape and limb darkening of KPD 1930. The uneven minima allow us to define the closest approach of the sdB star, and like Maxted et al. (2000), we define this as the zero-point of the orbital phase.

The light-curve maxima are also not quite even. Using the same Gaussian fitting technique, the maximum at $\phi_{\text{orb}} = 0.75$, which is when the sdB component is travelling towards us, is 0.06 ± 0.05 per cent brighter than at 1.25, when the star is travelling away from us. Doppler boosting and Doppler shifting affect the flux by a factor of $(1 - v(t)/c)$ (Maxted et al. 2000; G07) which, using K1 from G07, should result in a Doppler brightening semi-amplitude of 0.11 per cent. This is at the 1σ upper limit of our measurement. Instead of using the measured velocity to deduce flux differences in maxima, two of us (SDK and HP) attempted to constrain the velocity from the light curve itself. Using low-pass filtering of the light curve, we obtained approximate values for the flux increase and converted those to velocity. The estimate of the maximum radial velocity is $529.76 \pm 16 \text{ km s}^{-1}$ which is of the same order as the radial velocity measurements of G07. The error estimate is the error of the fit to the light curve and does not include the (large) systematic error of the spectrum estimate. [More details about this measurement and its effects on the binary will be discussed in Pablo et al. (in preparation).] So Doppler effects could be responsible for the difference in maxima. Interestingly, such special-relativistic effects have been detected in another sdB binary at the expected level (Bloemen et al. 2011).

3.2 Pulsation analysis

In a standard manner for long time-series data (i.e. Kilkenney et al. 1999; Reed et al. 2004b, 2007b), we analysed the data in several different groupings. We can use these groups to examine frequency and amplitude stability, look for consistent frequencies and amplitude variations. The groups are provided in Table 3, and pertinent sections of their temporal spectra [Fourier transforms (FTs)] are shown in Figs 5 and 6. Table 3 also lists the temporal resolution (defined as $1/t$, where t is the run duration) and the 4σ detection limit determined for ranges of 1000–3000 and 8000–10 000 μHz . Group I data include all of the XCov 23 data. Group II excludes

Table 3. Various groups of data used in our pulsation analysis. Columns 3 and 4 indicate the temporal resolution (in μHz) and 4σ detection limit (in mma).

Group	Inclusive dates	Resolution	Limit
I	Aug. 15–Sep. 9	0.45	0.44
II	Aug. 18–Sep. 7	0.60	0.31
III	Aug. 19–23	2.69	0.44
IV	Aug. 27–31	2.58	0.52
V	Sep. 3–6	3.75	0.77
VI	2002 July 10–21	1.87	0.59

noisy data, which is defined as a 4σ limit above 2 mma and has been trimmed so that for any overlapping data, only the best quality data were kept. Groups III, IV and V contain data obtained over 4 or 5 d of relatively good coverage during three different weeks of the 2003 campaign. Group VI is the 2002 small multisite campaign. Figure insets show the window functions, which are a single sine wave temporally sampled as the actual data. The central peak is the input frequency while other peaks are aliases which can complicate the data. Groups I and II are relatively well sampled, with alias peaks less than 40 per cent of the input amplitude whereas the remaining groups have obvious aliases that will contribute to the overall noise of the data.

A glance at the figures provides two simple observations as follows: (i) KPD 1930 is multiperiodic, pulsating in several tens of modes, confirming what was found in the discovery data (B00) and (ii) the pulsation frequencies are short-lived. This is evident from the fact that the highest amplitude peaks change between the shortest data sets (Groups III through VI) and the groups with the longest data sets (Groups I and II) have the lowest amplitudes.

As peak amplitudes in FTs show a mixture of the *median* amplitude and effects of phase stability, pre-whitening of the combined data sets could not be expected to accurately remove variations in amplitudes and/or phases (see Reed et al. 2007a; Koen 2009). However, because of the frequency density shorter duration data sets would likely have unresolved frequencies. This does not mean that least-squares fitting and pre-whitening are not of use; it is just that they need to be used with caution. We did the usual method of simultaneously fitting and pre-whitening the data using NLLS software independently for all the groups in Table 3 until we could not discern peaks (as in Fig. 7). However, because of the rich pulsation spectrum, we added an additional step. When searching the FT for pulsation peaks, we also plotted a window function made from the pre-whitening information gathered for all fitted frequencies. In this manner, we could view cumulative windowing effects and better judge the impact of pre-whitening on the FT. (A pre-whitening sequence of Group IV's data is provided as Fig. S1 in the online Supporting Information.)

Frequencies were deemed intrinsic to the star if they were detected in at least two groups above the 4σ detection limits. Table 4 provides a list of detected pulsation frequencies. The first column lists a designation, the second gives the frequency from the highest temporal-resolution group and the NLLS error is given in parentheses. Subsequent columns list the fitted amplitude from each group (NLLS error in parentheses) along with any pertinent notes: NF indicates that the frequency was not NLLS fitted, and frequencies fitted, but off by a daily alias, are noted as + or – for 1 daily alias away or ++ or –– for 2 daily aliases away. The last

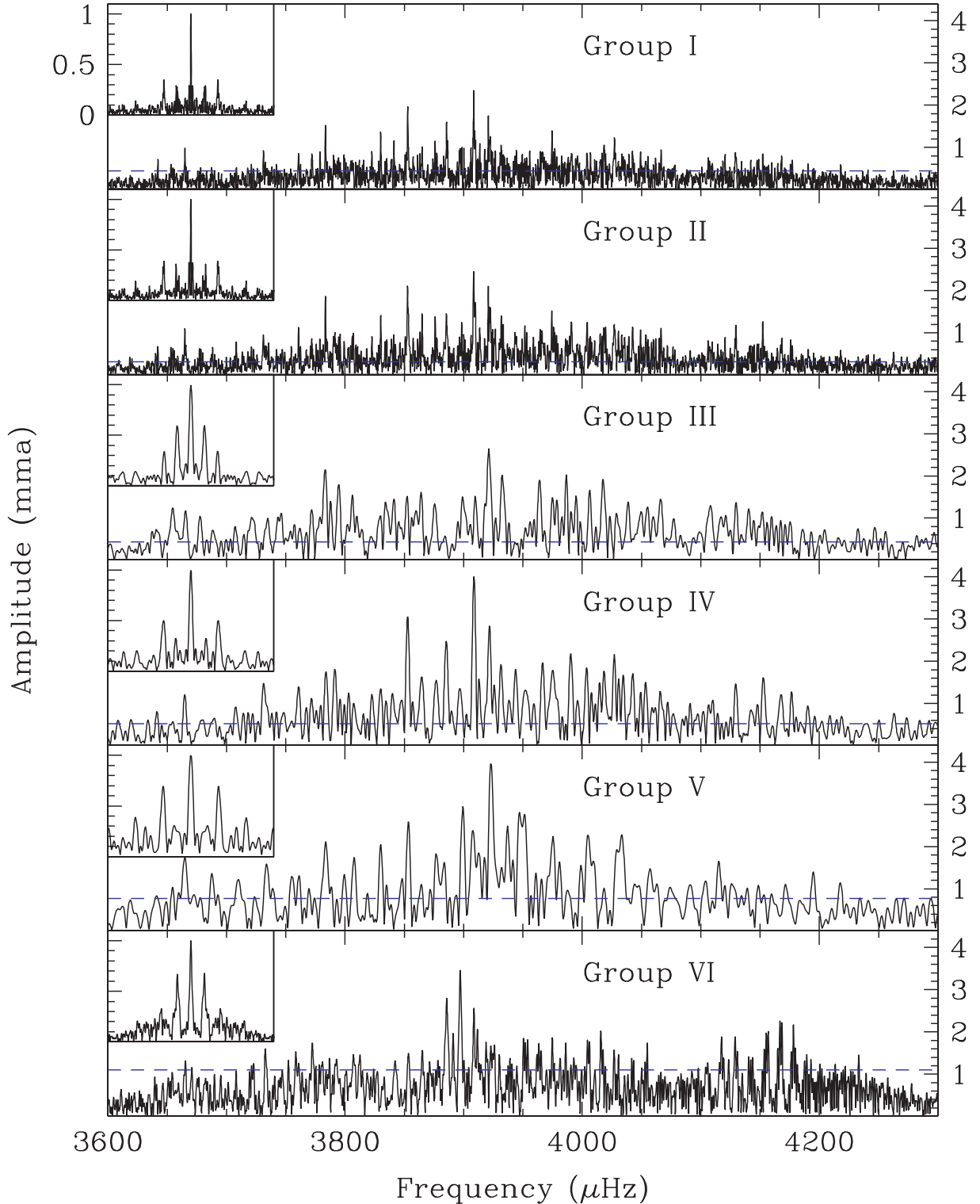


Figure 5. Plot of the temporal spectra and window functions (inset) for the groupings of data in Table 3 for the frequency range from 3600 to 4250 μHz . Dashed lines are the 4σ detection limit.

column notes other frequencies that are within 1 μHz of the daily alias as this could make pre-whitening difficult, depending on the window function. Table 5 lists other frequencies that we *suspect* are intrinsic to the star but did not meet our requirements. Fig. 7 is an expanded FT for Group II's data. Each panel shows the original FT and the residuals after pre-whitening. The dashed (blue) line is the

4σ detection limit. There are regions where the residuals remain higher than the 4σ detection limit because either NLLS fitting and pre-whitening did not effectively remove all of the amplitude (most likely caused by amplitude and/or phase variations or another, unresolved frequency) or remaining peaks were not observable in the original FT.

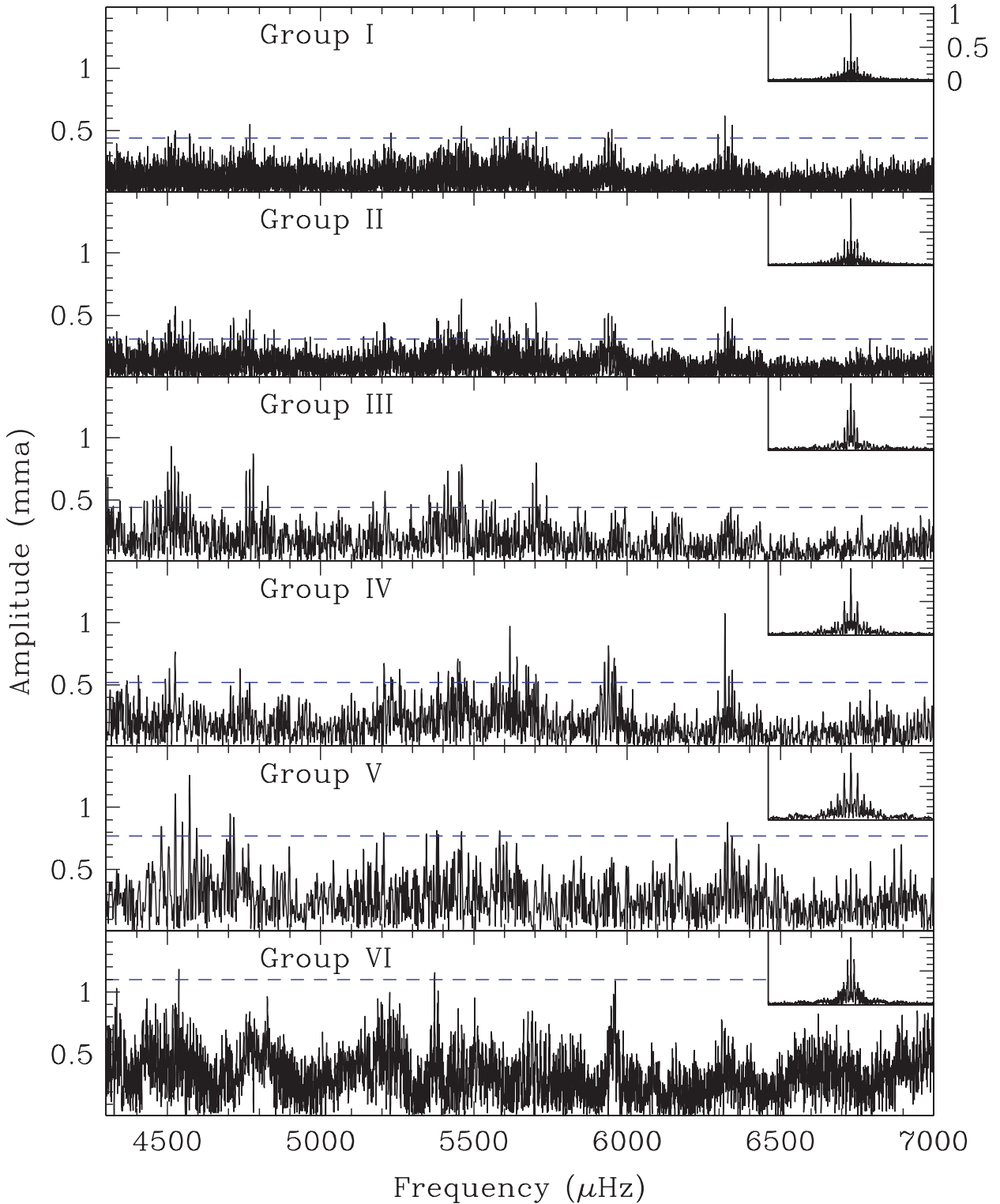


Figure 6. Same as Fig. 5 but for the frequency range from 4300 to 7000 μHz .

3.3 The frequency content

In total, we detected 68 independent pulsation frequencies and 13 suspected ones. Here we summarize some generalities which will be used in subsequent sections. Only three frequencies are detected in all six data groups. Six other frequencies are de-

tected in five data groups and 13 are detected in four data groups. 38 frequencies are within a 650- μHz region between 3650 and 4300 μHz . Unlike most sdBV stars, which contain several frequencies above 3 mma, KPD 1930 does not have any in the integrated data (Groups I and II). Only f_{17} has an amplitude of >2 mma in all detections, though it is only detected in four groups. 11 of the 68

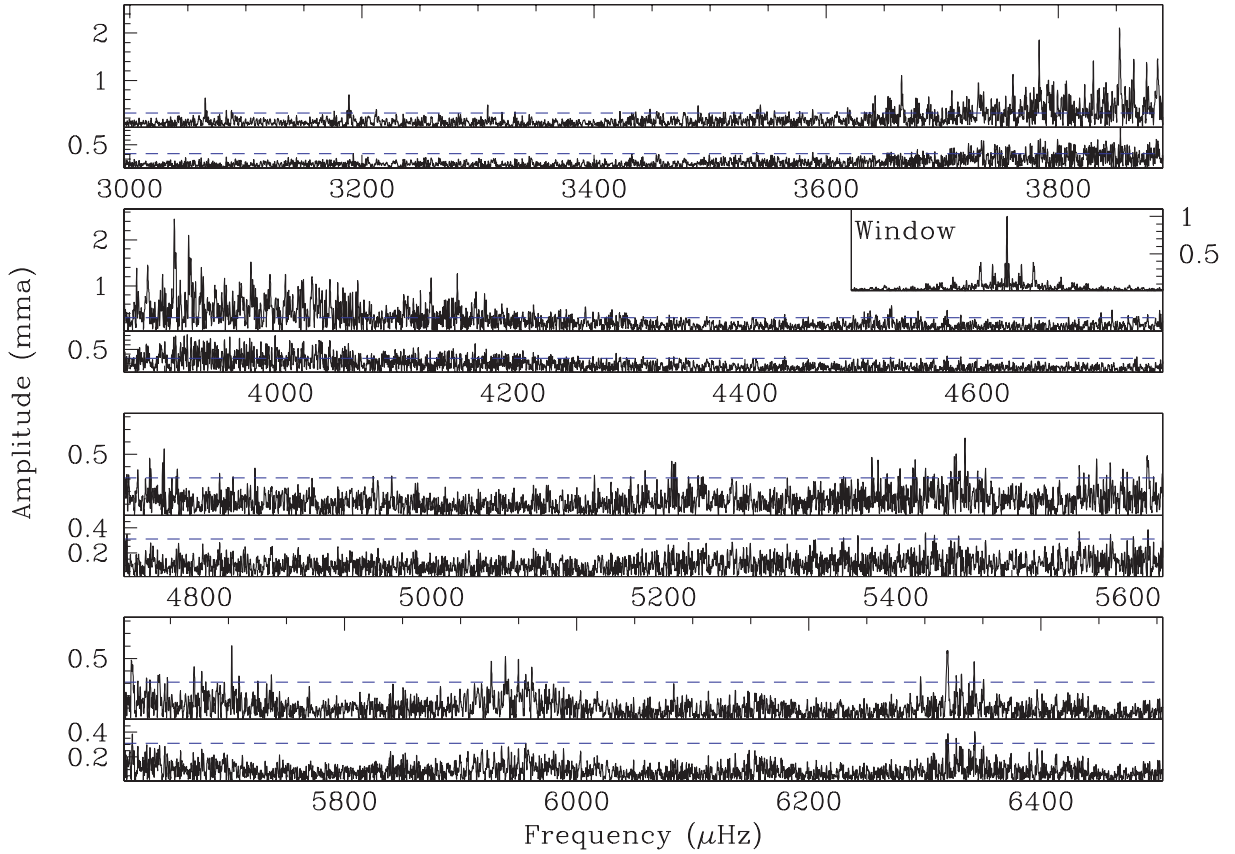


Figure 7. A detailed FT of Group II data showing the residuals after pre-whitening by 61 frequencies. Each panel shows the same frequency resolution, but the amplitudes in the top two panels differ from the bottom two. The dashed (blue) line is the 4σ detection limit.

frequencies have Group I amplitudes of > 1 mma and these always have higher amplitudes in the shorter data sets (Groups III through VI), if detected. These simple observations again lead to the conclusion that pulsations of KPD 1930 are highly variable in amplitude and/or phase over the course of our observations. Combining this with the density in the main region of pulsations will make accurate deciphering of the temporal spectrum difficult. Additionally, the pulsations in uncrowded regions have low amplitudes which will make them difficult to detect in short data sets.

4 DISCUSSION

4.1 Comparison with the discovery data

By combining their four nights of data, B00 obtained a resolution of $1.89 \mu\text{Hz}$ and their estimate of a mean noise level is 0.021 per cent, giving their data a 4σ detection limit of 0.84 mma. By comparison, our XCov 23 data have $4.2 \times$ better resolution and our detection limit is about half. Frequencies that match those of B00 are marked with a $^\circ$ in Tables 4 and 5 while those that are a daily alias away are marked with a $*$. 26 of our 81 frequencies are related to the 44 frequencies listed in B00. Of the eight frequencies listed in B00 with amplitudes greater than 2 mma, seven are detected in our data. For comparison, there are 21 frequencies which we have detected in at least five of our groups or have amplitudes of > 1 mma in at least two groups (one of which must be Group I or II), and of these, eight are related to frequencies detected in B00. This also indicates a substantial amount of amplitude and/or phase change since the B00 observations.

4.2 Amplitude and phase stability

KPD 1930 shows characteristics similar to the sdBV star PG 0048+091 (Reed et al. 2007b), which has pulsation properties normally associated with stochastic oscillations. These properties include frequencies that are inconsistent between data sets and lower amplitudes in longer duration data. Of the 69 frequencies in Table 4, only f_{10} , f_{11} and f_{24} are detected in all six groups of data, while f_2 is detected in five groups, with a peak just below 4σ in the sixth. Six more frequencies are detected and fitted in five of the six groups. Unfortunately, unlike PG 0048+091's well-spaced frequencies, most of those in KPD 1930 are packed tightly between 3600 and 4200 μHz . Outside of this main region of power, the amplitudes are quite low, making detection difficult.

Despite these complications, we analysed data sets of varying lengths with the goal of reaching time-scales shorter than the time-scale of amplitude and/or phase variations. Such data would be free of the resultant complications, allowing the amplitudes and phases to be more accurately measured. These could then be examined over the duration of our observations for changes. For the shortest possible time-scale, we examined every individual run for which the 4σ detection limit was better than 2.0 mma, totalling 32 runs. We also created 13 daily data sets combining low-noise runs that were contiguous or nearly so. The lengths of the daily data ranged from 7 to 27 h, with a median value of 16.5 h. Including the data for Groups III, IV and V, we have data sets sampling time-scales near 0.25, 0.67 and 4 d.

To resolve frequencies from individual runs and daily data sets, we selected frequencies isolated by at least $30 \mu\text{Hz}$ from Table 4

Table 4. Frequencies and amplitudes detected in various groupings of data. The temporal resolution of 1/(run length) and the 4σ detection limit are provided in the first two rows. Frequencies are in μHz and amplitudes in mma with NLLS fitting errors given by the last digits in parentheses. The last column indicates other frequencies that are within 1 μHz of the daily alias.

ID	Group	I	II	III	IV	V	VI	Alias
	4σ limit	0.44	0.31	0.44	0.52	0.77	0.59	
	resolution	0.45	0.60	2.69	2.58	3.75	1.87	
Amplitudes								
f1	3065.085 (49)	0.70 (8)	0.62 (8)	0.56 (13)	0.75 (13)	—	0.79 (14)	
f2*	3188.864 (44)	0.68 (8)	0.69 (8)	0.62 (13)	0.88 (13)	<4σ	0.61 (14)	
f3	3308.382 (66)	0.44 (8)	0.45 (8)	NF	<4σ	<4σ+	0.63 (14)+	
f4	3422.386 (92)	—	0.32 (8)	—	—	—	0.56 (14)+	
f5	3489.608 (80)	0.48 (8)	0.38 (8)	—	<4σ	—	—	
f6	3543.258 (60)	0.52 (8)	0.50 (8)	—	0.75 (13)	—	—	
f7	3653.074 (54)	0.55 (8)	0.59 (9)	1.13 (14)	—	—	—	f8
f8	3664.968 (29)	≈0.92 (9)	1.10 (9)	—	1.09 (14)	1.91 (24)	1.25 (15)	f7
f9	3683.269 (63)	0.41 (8)	—	≈0.95 (14)	—	—	1.17 (16)	
f10°	3731.065 (38)	0.84 (9)	0.79 (8)	1.40 (14)+	1.08 (15)	1.15 (24) ++	1.06 (16)−	
f11°	3783.460 (17)	1.51 (9)	1.88 (9)	2.35 (14)	1.84 (15)	1.52 (26)	1.55 (19)	
f12	3791.545 (41)	NF	0.79 (9)	—	NF	—	1.15 (19)+	
f13°	3804.693 (41)	—	0.79 (9)	—	—	—	1.67 (17)	
f14	3822.646 (39)	0.70 (9)	NF	1.28 (14)+NF	0.90 (15)++	≈1.96 (26)	—	
f15*	3852.709 (19)	1.64 (9)	1.90 (9)	1.63 (14)	2.27 (15)	NF	—	f16
f16	3862.952 (34)	—	1.06 (9)	NF	—	—	1.57 (16)	f15
f17*	3908.614 (17)	2.26 (11)	2.09 (9)	—	3.76 (15)	—	2.85 (17)−	f18
f18	3920.717 (27)	1.07 (10)	1.40 (10)	NF	NF	NF	1.04 (16) ^a	f17
f19	3921.901 (28)	1.22 (9)	1.29 (9)	2.40 ^a (14)	—	—	—	
f20	3924.426 (26)	1.30 (9)	1.24 (9)	—	—	3.94 (25) ^a	—	
f21	3926.008 (25)	1.11 (9)	—	—	—	—	1.77 (16)	
f22	3958.804 (35)	~0.66 (9)	0.94 (9)	—	—	—	—	
f23	3964.686 (30)	0.93 (9)	—	1.72 (15)	—	—	—	f24
f24°	3974.320 (19)	1.60 (9)	1.68 (9)	≈1.29 (15)	1.97 (15)	3.16 (25)	1.76 (16)	f23
f25°	3990.848 (29)	0.65 (9)	1.12 (9)	≈1.04 (16)	1.99 (15)	≈1.74 (25)	—	
f26	4004.192 (25)	—	1.31 (9)	—	—	2.01 (25)	—	
f27	4018.289 (27)	1.22 (9)	1.19 (9)	1.85 (14)	1.51 (15)	—	2.11 (16)	s72
f28	4027.241 (27)	1.04 (9)	—	NF	2.19 (16)	—	—	
f29	4034.710 (31)	0.90 (9)	—	—	1.37 (16)	—	—	
f30	4049.223 (29)	0.86 (9)	1.12 (9)	1.23 (14)	1.27 (15)	—	—	
f31*	4066.443 (33)	0.84 (9)	0.98 (9)	1.21 (14)	—	NF	—	
f32°	4120.459 (48)	0.78 (9)	0.65 (8)	—	NF	≈1.57 (24)	1.41 (16)−	
f33	4129.667 (32)	0.69 (9)	0.95 (9)	1.34 (13)	—	—	1.59 (16)	
f34*	4152.155 (33)	0.55 (9)	0.92 (9)	≈1.02 (13)	1.42 (14)	—	—	
f35	4168.331 (36)	0.92 (9)	0.85 (8)	—	1.19 (14)	—	1.81 (15)+	
f36°	4195.364 (51)	0.65 (9)	0.59 (8)	—	0.75 (14)	1.03 (22)	0.98 (14)	
f37°	4262.566 (69)	—	0.44 (8)	—	0.57 (14)	—	—	
f38	4297.849 (58)	0.44 (8)	0.43 (8)−	0.76 (17)	0.57 (13)	—	—	s75
f39°	4453.34 (31)	—	—	0.66 (13)	—	—	0.62 (14)−	
f40	4480.61 (57)	—	—	—	—	0.78 (22)	0.89 (14)	
f41	4507.884 (62)	—	0.48 (8)	0.50 (13)−	—	NF	0.57 (15)+	
f42	4524.708 (56)	0.66 (8)	0.53 (8)	0.99 (13)−	0.70 (13)	—	0.61 (14)	
f43	4549.152 (69)	—	0.44 (8)	0.49 (13)	—	—	—	
f44	4572.412 (42)	0.61 (8)	NF	0.51 (13)−	—	1.2 (22)	—	
f45	4716.271 (67)	NF	0.45 (8)	—	0.60 (13)++NF	0.98 (22)	NF−	
f46	4769.657 (67)	0.53 (8)	0.45 (8)	0.58 (14)−	—	—	—	f47
f47°	4781.042 (94)	—	0.31 (8)	0.67 (14)	—	—	—	f46
f48	4847.885 (84)	—	0.35 (8)	0.55 (13)−−	—	—	0.65 (14)−	
f49	5184.009 (86)	—	0.34 (8)	—	—	—	0.64 (14)	
f50	5207.451 (68)	NF	0.44 (8)	NF	0.67 (13) ^a	<4σ ^a	—	
f51*	5210.203 (78)	—	0.38 (8)	0.50 (13) ^a	—	—	—	
f52	5230.003 (41)	0.63 (8)	—	—	—	NF++	0.51 (14)++	
f53*	5379.426 (79)	—	0.38 (8)	0.57 (13)−−	—	—	—	
f54	5384.750 (83)	—	0.36 (8)	—	0.57 (13)	0.71 (22)	0.93 (14)+NF	
f55°	5416.641 (74)	—	0.40 (8)	0.72 (13)	≈0.65 (14)++	—	—	
f56	5451.930 (57)	—	0.53 (8)	0.72 (17)	0.73 (14)	NF	≈0.58 (15)	
f57	5459.529 (47)	0.51 (8)	0.64 (8)	≈0.56 (17)	—	<4σ	0.57 (15)	
f58*	5529.22 (37)	—	—	0.54 (13)	—	—	—	

Table 4 – continued

ID	Frequency	I	II	III	IV	V	VI
<i>f</i> 59	5572.909 (74)	–	0.40 (8)	≈0.51 (13)	–	0.72 (22)+	–
<i>f</i> 60	5616.391 (65)	0.51 (8)	0.46 (8)	–	0.94 (13)	NF	–
<i>f</i> 61	5670.540 (79)	–	0.38 (8)	–	0.64 (13)	–	≈0.61 (14)
<i>f</i> 62	5702.901 (51)	NF	0.59 (8)	0.98 (13)	–	–	0.79 (15)
<i>f</i> 63	5709.319 (79)	–	0.38 (8)	–	–	–	0.56 (15)+
<i>f</i> 64 [◊]	5737.037 (83)	<4 σ	0.35 (8)	0.47 (13)+	–	–	–
<i>f</i> 65	5938.582 (60)	0.42 (9)	0.54 (8)	–	0.74 (13)	–	0.51 (14)–
<i>f</i> 66 [◊]	5950.308 (68)	0.44 (9)	–	<4 σ +	≈0.61 (13)	–	≈0.74 (15)
<i>f</i> 67	6319.148 (69)	0.54 (9)	0.44 (8)	–	1.03 (13)	0.83 (22)+	1.40 (22)+
<i>f</i> 68	6342.994 (62)	0.52 (9)	0.49 (8)	<4 σ –	–	–	0.75 (22)

Note. + indicates that the frequency fit using NLLS was one daily alias (11.5 μ Hz) larger than that listed. Likewise, ++, – and –– indicate frequencies that are +2 daily, –1 daily and –2 daily aliases from those listed, respectively. ≈ indicates that frequencies were slightly more than 1 σ away from that shown, <4 σ indicates frequencies that had power in the FT which was below the 4 σ detection limit; NF indicates frequencies above the 4 σ limit that could not be fitted using our NLLS programme. ◊ indicates frequencies that match B00 while ★ indicates those that are a daily alias away.

^aUnresolved frequencies. Amplitudes of unresolved frequencies do not reflect the intrinsic amplitudes of each frequency.

Table 5. Same as Table 5 for suspected frequencies.

	Group	I	II	III	IV	V	VI	Alias
<i>s</i> 69	3448.361 (85)	–	0.35 (8)	–	–	–	–	
<i>s</i> 70 [◊]	3885.715 (28)	1.03 (10)	–	–	–	≈NF	–	
<i>s</i> 71	3995.235 (27)	1.01 (9)	–	–	–	NF	–	
<i>s</i> 72	4030.437 (29)	1.09 (9)	–	–	NF	NF	–	<i>f</i> 27
<i>s</i> 73	4232.67 (25)	–	–	0.91 (14)	–	–	–	
<i>s</i> 74	4246.23 (31)	–	–	0.74 (14)	–	–	–	
<i>s</i> 75★	4307.84 (29)	–	–	0.87 (17)	–	–	–	<i>f</i> 38
<i>s</i> 76	4897.000 (78)	–	0.38 (8)	–	–	–	–	
<i>s</i> 77	4949.582 (94)	–	0.31 (8)	–	–	–	–	
<i>s</i> 78	4965.63 (10)	–	0.36 (8)	–	–	–	–	
<i>s</i> 79 [◊]	5140.42 (12)	–	0.25 (8)	–	–	–	–	
<i>s</i> 80	5769.48 (11)	–	0.28 (8)	–	–	–	≈0.55 (14)	
<i>s</i> 81★	6083.547 (83)	–	0.35 (8)	<4 σ +	–	–	–	

which included *f*1 through *f*6, *f*44, *f*45, *f*48, *f*58 through *f*61, *f*67 and *f*68. We then attempted to fit amplitudes and phases for each of the frequencies for all of the data subsets. As expected, most of the fits failed as the pulsation amplitudes were well below the detection limits. Only for five frequencies were we able to fit phases and amplitudes to some of the shorter data sets. From the 48 data subsets, we fitted 52 of the possible 480 phases and amplitudes for the five frequencies. Phases are determined as the time of the first maximum amplitude after BJD = 245 2871.5 and converted to fractional phases by dividing by the period. In this manner, an error of 0.1 represents a 10 per cent change in phase. The fractional phases and amplitudes are shown in Figs 8 and 9 (and provided in Table S1 in the online Supporting Information). Horizontal bars indicate the time-span of the data for the daily and group sets. Note that some of the amplitudes are just below the 4 σ detection limit. We include them because the peaks were fairly obvious in the FT and since the frequency is known, a lower detection limit is not unreasonable.

Table 6 examines the amplitude and phase properties organized by the time domain. While *f*1 is not detected in any individual runs, the phase is stable to within the error bars. *f*2 shows deviations of 12 per cent and *f*44, *f*60 and *f*67 have deviations all near 18 per cent. Phase errors for individual measurements are under 10 per cent (except for one) with an average of 5.0 per cent. Phase variations are provided in Table 6 labelled as σ_ϕ (per cent). While the deviations

appear similar for *f*44, *f*60 and *f*67, *f*44 has one discrepant value while *f*60 and *f*67 appear as a phase variable, particularly from the individual runs (black circles in Fig 8). However none of the phases appear randomly distributed nor do they appear bimodal, which would be an indicator of unresolved frequencies.

The amplitudes show a larger variety. *f*1 and *f*2 are the most stable (the smallest $\sigma A/\langle A \rangle$), but the amplitudes for *f*1 are so small that it is not detected in any individual runs and only three of 13 daily runs. As such, it is clear that the number of detections will significantly affect amplitude stability as smaller and therefore more deviant amplitudes will not have been measured. For these five frequencies, none is detected more than 30 per cent of the time. Therefore our measure of amplitude variability, $\sigma A/\langle A \rangle$, should be considered a lower limit. Likewise, the variations for *f*44, *f*60 and *f*67 must be higher than what we report as they have some relatively high amplitudes yet are not detected in all runs. For the amplitudes, temporally nearby runs can have different amplitudes and consistently longer time domains have lower amplitudes. As these frequencies are reasonably separated from others for all of the time-scales considered and their amplitudes do not appear bimodal, it is unlikely that beating plays a role in the amplitude variations. They are most likely intrinsic to the pulsations.

The original goal of this subsection was to determine the time-scale of phase and amplitude variations. Indicators of this time-scale are the standard deviations, the ratios between of the average

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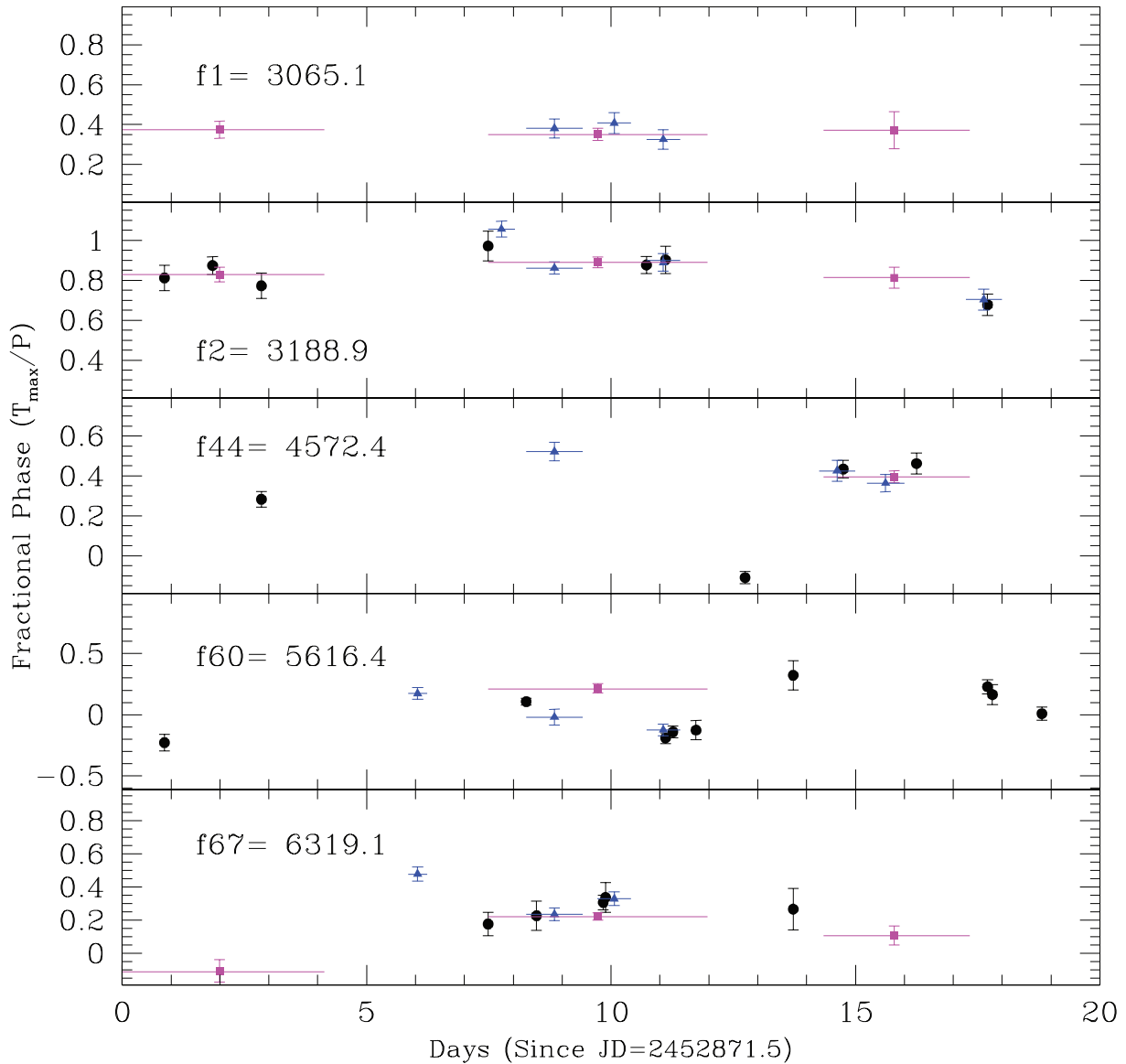


Figure 8. Phases of frequencies resolvable from short data sets. Circles (black) indicate individual runs, triangles (blue) are from daily runs and squares (magenta) are for Groups III to V. Horizontal lines indicate the time-span of the data used in the phase determination for the daily and group sets.

to maximum amplitudes and comparison these between the sets. For example, if the time-scale of variation is longer than a day, then the average and maximum values of the daily runs and the individual ones should be similar and should have $\langle A \rangle / A_{\max}$ near 1. For f_2 , the average daily amplitude is slightly larger than that for the individual runs while that for the group sets is significantly smaller. This indicates that the time-scale for amplitude variations is near to or longer than 16 h but shorter than 72 h.

4.3 Stochastic properties

An indicator for stochastic pulsations in solar-like oscillators is a $\sigma_A / \langle A \rangle$ ratio near 0.52 (Christensen-Dalsgaard, Kjeldsen & Mattei 2001). Pereira & Lopes (2005) also derived this ratio and were the first to apply it in testing whether pulsating sdB stars could be stochastically excited. Their results for the pulsating sdB star

PG 1605+072, based on seven nights of data, indicated that those pulsations were driven rather than stochastically excited. The ratios for f_{60} and f_{67} are near to this value. However in solar-like oscillators the amplitude decay time-scale is long compared to the re-excitation time-scale, and so this ratio may not be a good indicator for sdBV stars. Other features that could indicate stochastic oscillations include significant amplitude variability, amplitudes that are reduced in longer duration data sets (caused by phase variations) and match with simulated stochastic data.

Similar to what was done for PG 0048+091, we produced Monte Carlo simulations for stochastic oscillations with varying decay and re-excitation time-scales appropriate for the various data sets and groups we had for KPD 1930. As there are many amplitude ratios to work with from Table 6, it was hoped that tight constraints for amplitude variations could be deduced by matching the simulations with the observations. However, such was not the case and the

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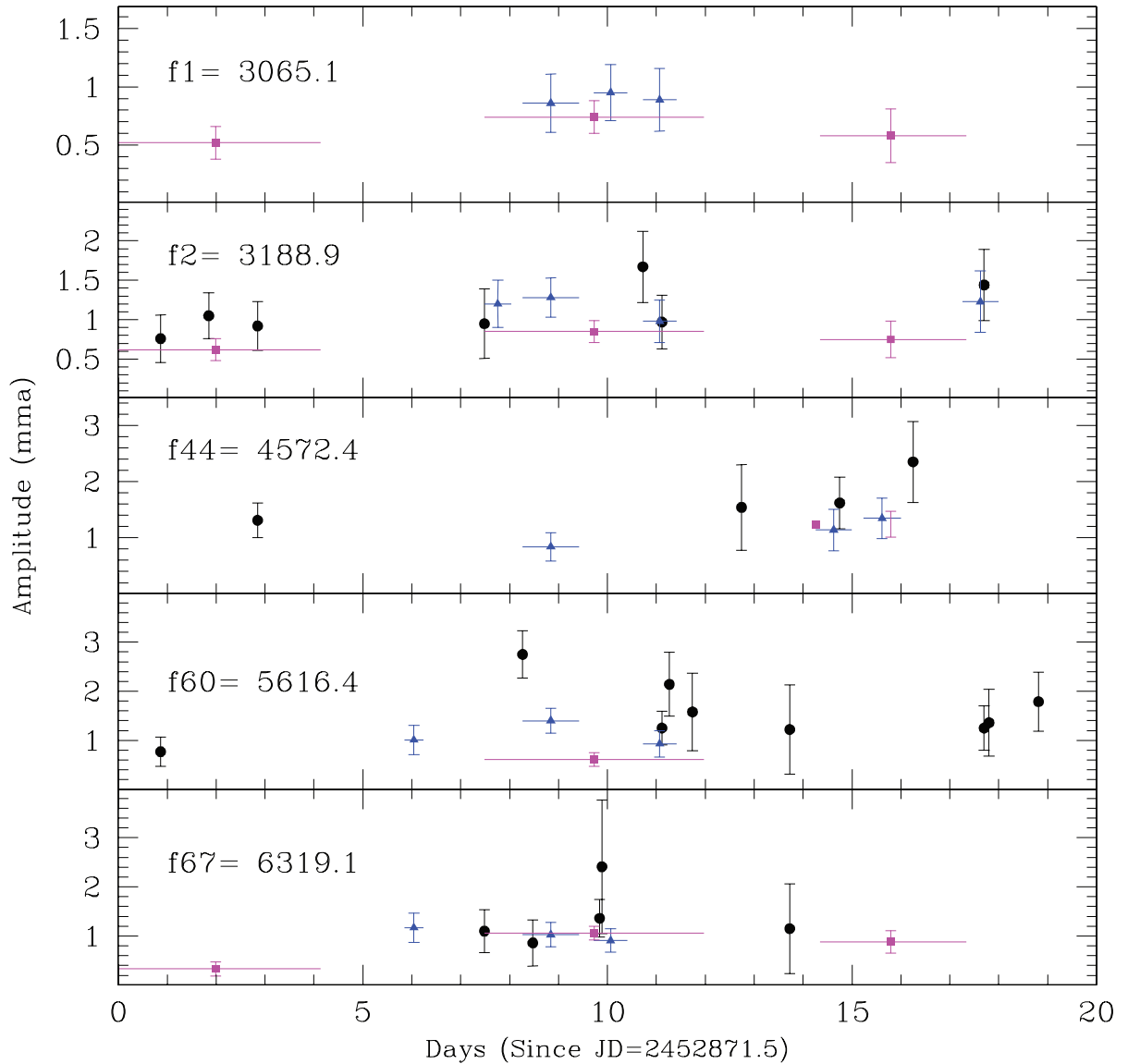


Figure 9. Pulsation amplitudes corresponding to the phases shown in Fig. 8.

best we could do was produce loose time-scales. The best results for f_1 indicate short amplitude decay time-scales (4–6 h) and long re-excitation time-scales (20–30 h), those for f_2 indicate medium decay time-scales (9–15 h) and medium to long re-excitation time-scales (12–27 h), those for f_{44} indicate short decay time-scales (4–9 h) and medium re-excitation time-scales (8–16 h), those for f_{60} indicate short to medium decay time-scales (4–15 h) and long re-excitation time-scales (25–40 h), and those for f_{67} indicate short to medium decay time-scales (4–20 h) and long re-excitation time-scales (15–28 h). The resultant time-scales are fairly consistent in that the decays are always short compared to the re-excitations, but they are not nearly as clear as for PG 0048+091, certainly owing to the complexity of KPD 1930’s pulsation spectrum. However, the pulsation phases do not appear randomly distributed, as would be expected for stochastic oscillations. So we are left with some indications that stochastic processes may be present and some information contrary to stochastic oscillations. From these data, we cannot discern between them.

4.4 Observed multiplets

From the ellipsoidal variations in KPD 1930, we can strongly infer it to be tidally locked, which means that we also know the rotation period. In standard spherical harmonics, each ℓ can produce $2\ell + 1$ m azimuthal values separated by the orbital frequency and the Ledoux constant (which is very small for p modes in sdB stars). We can search for multiplets to impose observational constraints on the mode degrees (ℓ). Table 7 lists multiplets detected to splittings of four times the orbital frequency of 121.7 μHz . As there are many pulsation frequencies related by a multiple of the rotation/orbital frequency, the order of the frequencies is the same as in Table 4 with the numbers in parentheses indicating the multiple of the rotation/orbital frequency between it and the previous (smaller) frequency. The leftmost frequency is just the lowest for each multiplet but has no significance otherwise.

Table 6. Properties of pulsation phases and amplitudes for frequencies separated by >30 μHz . Pulsation amplitudes are compared in a number of ways including by standard deviations (σ), average ($\langle \rangle$) and maximum ($_{\text{max}}$) amplitudes for various groupings of data. The number of possible detections is in parentheses next to the category (All, Individual, Daily or Groups).

	$f1$	$f2$	$f44$	$f60$	$f67$
All (54)					
$\#_{\text{det}}$	7	16	8	14	16
$\langle A \rangle$	0.79	1.07	1.43	1.33	1.04
σ_A	0.19	0.27	0.45	0.60	0.45
$\sigma_A / \langle A \rangle$	0.24	0.25	0.31	0.45	0.43
$A_{\text{GI-II}} / \langle A \rangle$	0.78	0.64	0.43	0.35	0.42
σ_ϕ (per cent)	4.3	12.4	19.7	17.8	17.1
Individual runs (37)					
$\#_{\text{det}}$	0	8	4	10	9
$\langle A \rangle$	–	1.11	1.72	1.47	1.20
σ_A	–	0.29	0.45	0.64	0.51
$\sigma_A / \langle A \rangle$	–	0.26	0.26	0.44	0.43
A_{max}	–	1.67	2.35	2.75	2.41
$\langle A \rangle / A_{\text{max}}$	–	0.66	0.73	0.53	0.50
$A_{\text{GI-II}} / \langle A \rangle$	–	0.62	0.35	0.31	0.37
$\langle A_d \rangle / \langle A \rangle$	–	1.05	0.65	0.76	0.87
$\langle A_{\text{GIII-VI}} \rangle / \langle A \rangle$	–	0.79	0.72	0.41	0.59
$A_{\text{GI-II}} / A_{\text{max}}$	–	0.41	0.26	0.17	0.18
$\langle A_d \rangle / A_{\text{max}}$	–	0.70	0.47	0.40	0.43
$\langle A_{\text{GIII-VI}} \rangle / A_{\text{max}}$	–	0.53	0.53	0.22	0.29
σ_ϕ (per cent)	–	14.6	26.0	19.2	13.6
Daily runs (13)					
$\#_{\text{det}}$	3	4	3	3	3
$\langle A \rangle$	0.90	1.17	1.11	1.11	1.04
σ_A	0.05	0.13	0.26	0.25	0.13
$\sigma_A / \langle A \rangle$	0.06	0.11	0.23	0.23	0.13
A_{max}	0.95	1.28	1.35	1.40	1.17
$\langle A \rangle / A_{\text{max}}$	0.95	0.91	0.82	0.79	0.89
$A_{\text{GI-II}} / \langle A \rangle$	0.69	0.59	0.55	0.41	0.42
$\langle A_{\text{GIII-VI}} \rangle / \langle A \rangle$	0.79	0.75	1.12	0.55	0.68
$A_{\text{GI-II}} / A_{\text{max}}$	0.65	0.54	0.45	0.33	0.38
$\langle A_{\text{GIII-VI}} \rangle / A_{\text{max}}$	0.75	0.69	0.92	0.44	0.61
σ_ϕ (per cent)	4.0	14.5	8.0	15.2	12.2
Groups III–VI					
$\#_{\text{det}}$	4	4	1	1	4
$\langle A \rangle$	0.71	0.88	1.24	0.61	0.71
σ_A	0.22	0.29	–	–	0.33
$\sigma_A / \langle A \rangle$	0.31	0.33	–	–	0.46
A_{max}	1.01	1.28	1.24	0.61	1.06
$\langle A \rangle / A_{\text{max}}$	0.70	0.69	–	–	0.67
$A_{\text{GI-II}} / \langle A \rangle$	0.87	0.78	0.49	0.75	0.62
$A_{\text{GI-II}} / A_{\text{max}}$	0.61	0.54	0.49	0.75	0.42
σ_ϕ (per cent)	4.9	3.4	–	–	14.0

4.4.1 Classical interpretation

In total, 61 of our 81 frequencies are related by a multiple of the rotation/orbital frequency. In a classical asteroseismological interpretation, we would assume that the spin axis is aligned with the orbital axis and the stars are tidally locked. As such, we are viewing the spin axis close to equator-on, or an inclination near 80° and the multiplets are caused by stellar rotation.

As each degree can have $2\ell + 1$ azimuthal orders, m , the number of orbital splittings provides a minimum ℓ value and constrains where the $m = 0$ is. For example, the $f1, f2, f3$ triplet is best interpreted as an $\ell = 1$ triplet with $m = 0$ at $f2$. The multiplet beginning with $f4$ has sufficient frequencies to warrant an $\ell = 3$

Table 7. Pulsation frequencies split by a multiple of the rotation/orbital frequency. The pulsation frequencies refer to those in Tables 4 and 5. The frequencies are in ascending order and the number in parentheses indicates the multiple of the orbital frequency between itself and the previously listed frequency. Column 1 lists the minimum degree for the multiplet using the classical interpretation.

ℓ_{min}	Des.	Designations of related frequencies
1	$f1$:	$f2$ (1), $f3$ (1)
1, 1 or 3	$f4$:	$f6$ (1), $f8$ (1), $f17$ (2), $s72$ (1), $f34$ (1)
2	$f5$:	$f10$ (2), $f15$ (1), $f24$ (1)
2 or 4	$f7$:	$f27$ (3), $f37$ (2), $f41$ (2)
2	$f9$:	$f13$ (1), $f21$ (1), $f30$ (1), $f35$ (1)
1	$f11$:	$f28$ (2)
1	$f12$:	$f29$ (2)
3	$f14$:	$f31$ (2), $s75$ (2), $f43$ (2)
1	$s70$:	$f33$ (2)
1 or 3	$f23$:	$f39$ (4), $f44$ (1)
2	$f25$:	$s73$ (2)
3 or 5	$s71$:	$f40$ (4), $f48$ (3), $f51$ (3)
1	$f26$:	$s74$ (2)
1	$f42$:	$f46$ (2)
2	$s76$:	$s79$ (2), $f55$ (2)
4 or 3	$s78$:	$f50$ (2), $f56$ (2), $f59$ (1), $f65$ (3)
2	$f49$:	$f61$ (4)
1	$f57$:	$f62$ (2)
1	$f60$:	$f64$ (1)
1	$f63$:	$f66$ (2)

interpretation. However, $\ell = 3$ modes have low amplitudes caused by geometric cancellation, making such an interpretation unlikely. More feasible is the fact that there are two $\ell = 1$ multiplets with their outside components at a chance separation of nearly $2f_{\text{orb}}$. Column 1 of Table 7 gives the minimum ℓ degree based on the number of orbital splittings. For entries with multiple possibilities, the most likely is given first. (The online Supporting Information includes a colour-coded figure showing the multiplets and a figure showing just the $m =$ components with their corresponding degrees; Figs S2 and S3.)

We can also use the pulsation amplitudes to place some constraints on the modal degrees. Using Groups I and II as a guide, all of the amplitudes are within a factor of 7 of each other, while most are within a factor of 4. Table 8 lists the geometric cancellation factors for azimuthal orders $\ell, m = 1, 0$ through 4, 4 for rotation axes of $i_r = 70^\circ$ and 80° . These factors indicate how much a pulsation amplitude would be reduced relative to a radial mode, which suffers no geometric cancellation. As Column 2 indicates, for the classical interpretation, all of the $\ell \leq 2$ modes have amplitudes reduced by factors less than 5–8, depending on orientation. This is roughly in agreement with the observed amplitude range. By contrast, all $\ell \geq 3$ modes have amplitudes reduced by factors of ≥ 20 (except for $\ell, m = 4, |1|$ depending on the viewing angle). Since we do not observe this range of amplitudes in KPD 1930, it is unlikely that these multiplets are being observed.

Ignoring high-degree modes, there remains multiplets as evidence of 12 $\ell = 1$ and four $\ell = 2$ modes. There are also 20 frequencies which show *no* relations to other frequencies via an orbital overtone. These are all candidates for radial modes. As there is no geometric cancellation for radial modes, they would be expected to have some of the higher amplitudes. $f16, f18, f19$ and $f20$ all have amplitudes greater than 1 mma for all of their detections. Yet none of these has amplitudes significantly higher than the other frequencies.

Table 8. Geometric cancellation (pulsation amplitude reduction) factors for $i_r = 80^\circ$ ($i_r = 70^\circ$ in parentheses).

ℓ, m	Classical	Tipped
1, 0	4.81 (2.44)	1.69 (1.77)
1, 1	1.20 (1.26)	2.40 (2.52)
2, 0	3.35 (4.70)	4.18 (4.59)
2, 1	7.28 (3.87)	5.15 (5.65)
2, 2	2.57 (2.82)	5.48 (7.67)
3, 0	48.2 (28.9)	39.9 (45.9)
3, 1	32.9 (70.6)	860 (72.6)
3, 2	51.7 (28.9)	73.0 (57.8)
3, 3	22.3 (25.7)	68.1 (51.8)
4, 0	32.9 (7.911)	34.6 (41.8)
4, 1	41.7 (4.81)	7.46 (8.04)
4, 2	30.0 (151)	55.0 (45.9)
4, 3	173 (21.4)	64.2 (57.2)
4, 4	81.4 (98.1)	282 (218)

Therefore, it is also possible they are $\ell > 0$ modes with only one frequency visible.

4.4.2 Tipped-axis interpretation

Another interpretation would be that the pulsation axis is aligned with the tidal force of the companion. As described by Reed, Brondel & Kawaler (2005), such a pulsation geometry would precess, completing a revolution every orbital period. The change in viewing pulsation geometry incorporates three additional pieces of information into the light curve which can be used to uniquely identify the pulsation degree ℓ and the absolute value of the azimuthal order $|m|$. These are a pattern of peaks in the FT of the integrated light curve, two or more 180° flips in the pulsation phase over an orbital period and recovery of the ‘true’ peak in the FT of the phase-separated data. As in Reed et al. (2005), we will not seek analytic solutions, but will use simulated data of precessing pulsation geometries to guide us. These simulations and any tipped-axis analysis make the assumption that spherical harmonics apply.

We begin by searching for patterns in the FT of the integrated data of KPD 1930. To guide our search, we produced simulated data for modes from $\ell = 0$ to 4 for an orbital/rotation axis of $i_r = 70^\circ$ and a pulsation axis of $i_p = 85^\circ$ relative to the rotation axis. This geometry seems reasonable for what we know of the orbital inclination and with tidal forces larger than the maximum Coriolis force. Changes of 5° – 10° in either axis make little difference in the patterns. The simulated FTs are shown in Fig. 10. The amplitudes are relative to the $\ell = 0$ (radial) mode and along with the geometric cancellation factors of Table 8 indicate that high-degree modes are unlikely to be observed. The frequency patterns of Fig. 10 are what we are looking for in the observed data.

18 of the multiplets from Table 4 match patterns from simulated tipped-axis pulsations.² The next step is to divide the data into orbital regions of like and opposing pulsation phases [Reed et al. (2005) showed this procedure in detail] for the different modes. If the intrinsic frequencies predicted by the tipped-axis model are recovered, and their phases are opposite in appropriate data sets,

this would be a reasonable indicator of a tipped pulsation axis. As can be seen in Fig. 10, the intrinsic frequency for tipped modes $\ell, m = 1, 1; 2, 0; 2, 3, 1$ and $3, 3$ will have a corresponding frequency in the combined data. As such, recovering the peak in the divided data is less important but detecting a phase shift of 0.5 will be vitally important for associating these frequency patterns with tipped pulsation modes.

We separated the data for Groups I through V into orbital regions of like and opposing phases appropriate for modes $\ell, m = 1, 0$ through 4, 4 and searched each group not only for the frequencies predicted from the observed multiplets, but for any previously unobserved frequencies above the noise.³ The simplest data sets are those for $\ell = 1$ as the orbit is divided into halves, with set A of $\ell, m = 1, 1$ going from an orbital phase of 0.0 to 0.5 and set B covering the other half. Those for $\ell, m = 1, 0$ are shifted by -0.25 in phase. Table 9 provides the results of the search. Column 1 provides a unique mode identifier (with a corresponding identifier from Table 4 in parentheses, if there is any), Column 2 the frequency, Column 3 indicates the mode the data were phase-separated for and the remaining columns give the phase difference (set A – set B) for each group.

As anticipated considering the complexity of the data, the results are not straightforward. In the split data sets, the aliasing is significantly worse and the pulsation amplitudes are very low. Evidence also suggests that amplitudes and phases are changing throughout the campaign. Most of the predicted frequencies are not detected. Those that are detected have amplitudes only marginally above the noise. But the strongest evidence will be consistent phase differences of one-half in the various data sets. Frequency $t10$ ($f15$) shows no phase shift between the sets for all groups and so cannot be a tipped pulsation mode. Frequencies $t11$ and $t14$ have intermediate values, again indicating that they are likely not tipped pulsation modes, but rather that their phases are not stable over the course of the observations. Frequencies $t2$ and $t12$ are only detected in two of the five data sets, and while one phase difference is near one-half, the other has an intermediate value. As $t2$ is also detected in the integrated light curve, but should not be for an $\ell, m = 1, 0$ mode, it is unlikely a tipped mode. Frequencies $t5, t8$ and $t9$ do fit what we expect for tipped pulsations. $t9$ is detected with a similar phase difference in all five groups, $t8$ has consistent phase differences for the three data sets in which it can be detected and $t5$ has consistent phase differences in three of four detections. Additionally, $t5$ is not detected in the integrated data, as should be the case. More surprising are the results for $t17$ and $t19$, both of which are only detected in two of the five groups but have phase differences near to one-half. These modes are unlikely to be observed because the geometric cancellation factors are very high (73 and 282, respectively), meaning the intrinsic amplitudes would need to be much higher than the others. Monte Carlo simulations were produced with random phases between data sets. This could be appropriate for purely stochastic pulsations, but for driven pulsations, the phases should not be random at all, but rather close to a fixed number. As tipped pulsations have a phase shift of 0.5 which is very unexpected for driven pulsations, the significance of the simulations is somewhat startling. Our phase detections for $t8$ and $t9$ only occur in 0.1 per cent of our simulations while those for $t5$ occur 1.0 per cent of the time. Those for $t17$ and $t19$ occur 6.7 and 4.9 per cent of the time, respectively.

² These are shown schematically in Fig. S2 of the online Supporting Information.

³ The phased data sets for Group II with $\ell, m = 1, 0$ and $1, 1$ are shown in Fig. S5 of the online Supporting Information.

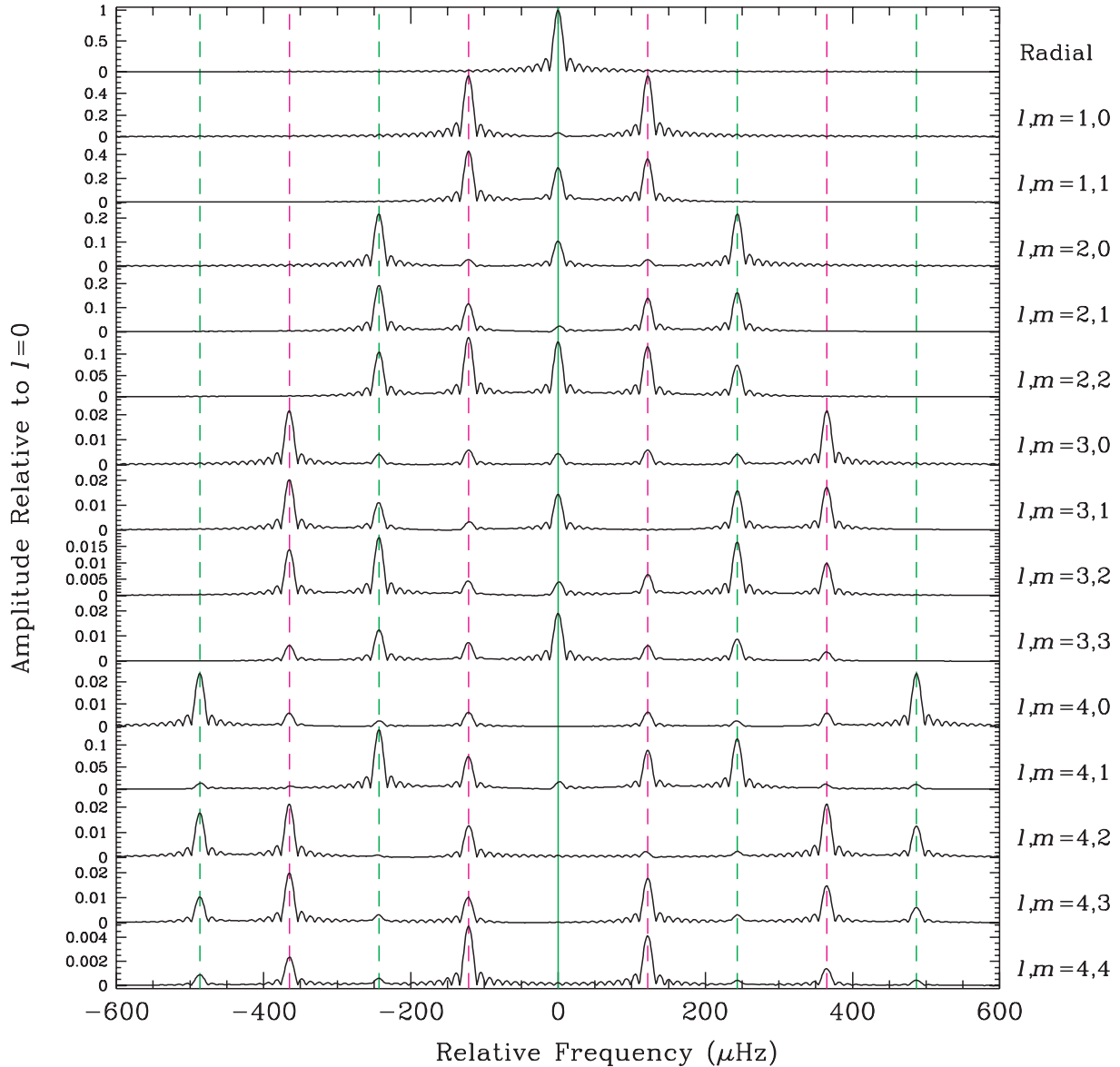


Figure 10. Pulsation spectra of simulated data where the pulsation pole points 5° off the orbital axis, which has an inclination of 70° . The input frequency is at the centre (solid green line) and the dashed lines indicate orbital aliases. The amplitudes are relative to the radial mode and the mode is indicated on the right-hand side.

Of the 18 frequency multiplets in the combined data sets, three possess indicators for tipped pulsation modes. Nine have no detections at all, two have phase differences near zero and two more have marginally appropriate phase differences, but would indicate modes that are unlikely to be detected because of geometric cancellation. Still, particularly for $\tau 5$, which is not observed in the integrated data, the phase difference is a precise indicator for tipped pulsation modes. The chance of this occurring randomly is quite small.

4.5 Orbital dependence

While searching for tipped-axis pulsations, we stumbled upon the unexpected finding that some frequencies appeared to only occur for some stellar orientations.⁴ So we divided the data into four, eight and

10 subsets according to the orbital phase and examined the pulsation spectra of each. We found that quadrants, centred around the orbital phases 0 (QI), 0.25 (QII), 0.5 (QIII) and 0.75 (QIV) sufficiently differentiated the orbital dependence of the frequencies. Temporal spectra of Group II's data, split into four quadrants, are shown in Fig. 11. The dashed lines indicate likely intrinsic frequencies while the dotted lines are more likely aliases, with the arrows indicating which frequency they are an alias of.

It is obvious that there is an orbital dependence on some frequencies, particularly $\phi 3$, which is clearly and only seen in QI. This most likely means that the pulsation geometry, as normally described by spherical harmonics, is more complex for these frequencies. Describing the pulsation geometry for such modes is beyond the scope of this paper, but we provide frequencies which have a detectable orbital dependence in Table 10. Outside of the main area of power, there is little sign of this uniqueness other than the fact that $f 57$ (5459) has a slightly higher amplitude in quadrant $\phi = 0.25$ and

⁴ These can be seen in Fig. S5 of the online Supporting Information.

Table 9. Phase differences (A–B) for possible tipped pulsation frequencies. NLLS errors are in parentheses. Differences near ± 0.5 indicate tipped-axis modes.

ID	Frequency	Mode	GI	GII	GIH	GIV	GV
<i>t1</i> (<i>f</i> 17)	3913	1, 0	–	–	–	–	–
<i>t2</i> (<i>f</i> 26)	4008	1, 0	–0.50 (2)	0.82 (2)	–	–	–
<i>t3</i> (<i>f</i> 32)	4113	1, 0	–	–	–	–	–
<i>t4</i> (<i>f</i> 33)	4126	1, 0	–	–	–	–	–
<i>t5</i>	4647	1, 0	0.55 (6)	–0.45 (5)	0.27 (4)	–0.43 (6)	–
<i>t6</i>	5581	1, 0	–	–	–	–	–
<i>t7</i>	5831	1, 0	–	–	–	–	–
<i>t8</i> (<i>f</i> 2)	3187	1, 1	–0.55 (3)	0.49 (5)	–	0.46 (4)	–
<i>t9</i> (<i>f</i> 6)	3543	1, 1	–0.67 (3)	–0.64 (3)	–0.51 (4)	0.39 (4)	0.41 (4)
<i>t10</i> (<i>f</i> 15)	3853	1, 1	–0.08 (3)	–0.07 (2)	–0.16 (3)	–0.01 (2)	–0.13 (3)
<i>t11</i> (<i>f</i> 28/29)	4030	1, 1	–0.25 (2)	–0.26 (2)	–	–0.39 (2)	–0.26 (3)
<i>t12</i> (<i>f</i> 37)	4263	2, 0	–	0.51 (2)	–	–0.31 (4)	–
<i>t13</i>	5140	2, 0	–	–	–	–	–
<i>t14</i> (<i>f</i> 10)	3731	2, 2	–0.22 (2)	–	–	–0.27 (2)	–
<i>t15</i> (<i>f</i> 21)	3926	2, 2	–	–	–	–	–
<i>t16</i> (<i>f</i> 50)	5207	3, 1	–	–	–	–	–
<i>t17</i>	4210	3, 2	–0.54 (5)	–	–	–0.63 (3)	–
<i>t18</i>	4188	4, 3	–	–	–	–	–
<i>t19</i>	4188	4, 4	0.61 (4)	–	–0.47 (5)	–	–

*f*67 (6319) is higher in quadrants $\phi = 0$ and 0.5. Undoubtedly, the lack of other detections is caused by low amplitudes combined with severe aliasing.

5 RESULTS

We have analysed WET data spanning 26 d in 2003 August and September, supplemented by 45 h of multisite data obtained in 2002 July. These data were used to examine the orbital properties and the pulsation spectrum of the sdB+WD binary KPD 1930. We used the ellipsoidal variation to affirm the orbital period and folded the data over that period. No signs of eclipse were detected, constraining the inclination to $< 78^\circ.5$. Additionally, we noted that the minima are uneven, indicating that KPD 1930 is very slightly asymmetric and marginally detect anticipated Doppler effects from possibly uneven maxima.

As implied from the discovery data (B00), we have found KPD 1930 to be an extremely complex pulsator with frequencies and amplitudes that can vary on a daily time-scale. In these data, we confidently detect 68 pulsation frequencies and suggest a further 13. Of these, only 26 are related to frequencies observed by B00, a surprisingly small number that attests to KPD 1930's pulsational complexity. Our WET data, which covered more than three weeks during 2003, have over four times better temporal resolution and one-half the detection limit of B00.

We examined amplitude and phase stability by analysing subsets of data over several time-scales for well-separated frequencies. Unfortunately, the low amplitude of these frequencies hampered our investigation and we were unable to detect them in most of the subsets. For the times we could detect them, we found the pulsation amplitudes to be fairly variable, although all $\sigma_A/\langle A \rangle$ ratios are short of the value of 0.52 used in solar-like oscillators to indicate stochastic oscillations (Christensen-Dalsgaard et al. 2001). The low ratio could be an artefact of only a few amplitude detections or caused by an amplitude decay time-scale shorter than the re-excitation time-scale. To investigate time-scales, we compared the observed amplitude ratios for several subsets with simulated stochastic oscillations. The simulations could easily fit the observed ratios and broadly found

decay time-scales near 12 h and re-excitation time-scales near 25 h. As such, the pulsations do have some qualities normally associated with stochastic oscillations; however, the phases are relatively stable which argue against stochastic oscillations. Hence, it is possible that the amplitude variations have a different cause.

We have found 20 separate multiplets including up to 61 frequencies. Assuming the classical interpretation which aligns the pulsation axis with the rotation axis, these would indicate 12 $\ell = 1$, four $\ell = 2$ and/or possibly (but unlikely) four $\ell = 3$, two $\ell = 4$ and one $\ell = 5$ modes. We also searched for indicators of a tidally induced tipped pulsation axis which would precess with each orbit. While the complexities of the pulsations made searching for tipped modes difficult, three frequencies were found which indicated that tipped modes are present.

Two further modes have indications of tipped modes, but these would indicate $\ell = 3$ and 4, which are unlikely to be observed. We also detected frequencies which only appeared during certain orbital phases, which indicate that some frequencies are affected by the slight asymmetry of the star. Fig. 12 schematically shows these results with the height of the arrows indicating the degree (except as noted below). Classically interpreted multiplet $m = 0$ components are shown as solid arrows (with multiple possible $m = 0$ frequencies connected by a horizontal line as in Fig. 10 and colour-coded in the electronic version); modes from the tipped-axis interpretation are shown as dashed arrows, with the m value above the arrow; and frequencies which only appear during certain orbital phases are shown as dotted arrows (at an arbitrary height of 1.5 since we have no indication of their degree). Any frequencies that were not involved in the above cases were (somewhat arbitrarily) deemed to be $\ell = 0$ modes and are indicated in the figure with solid arrows. Note that the classically interpreted $\ell = 1$ mode which could have its $m = 0$ component at 4453 or 4572 is marked with a question mark. This is part of the tipped $l, m = 3, 2$ multiplet and so if the tipped mode is correct, then the classical mode would be invalid. The small '3' and '2' under the axes are to indicate that there are three and two closely spaced frequencies, all of which fit the conditions we ascribe to $\ell = 0$ modes that would be unresolvable in the figure.

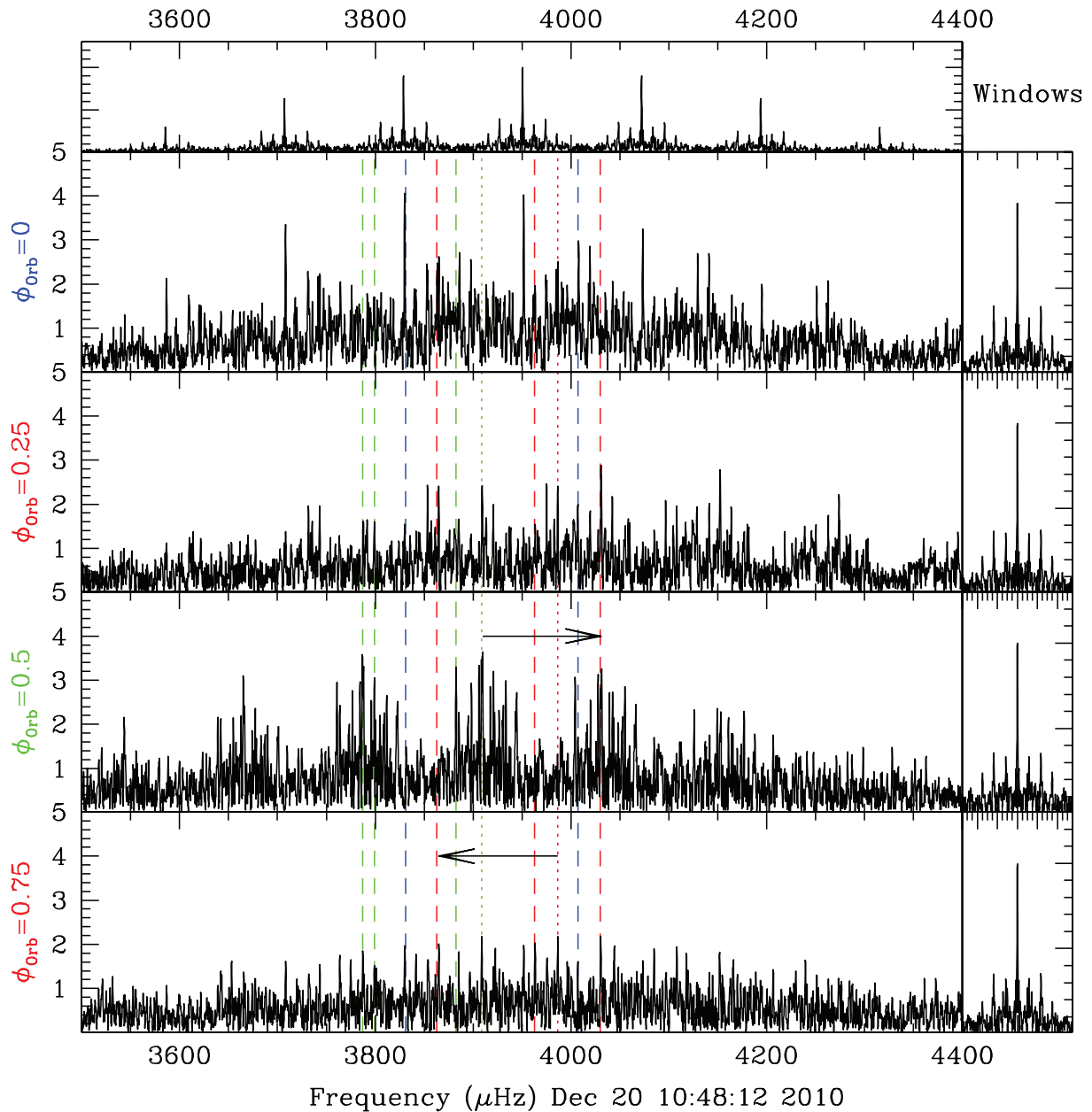


Figure 11. Pulsation spectra of Group II's data, separated into four subsets based on the orbital phase. Dashed lines indicate frequencies which show an orbital dependence and dotted lines indicate frequencies that are an orbital alias away from the most likely frequency (indicated with an arrow and colour-coded in the online version). The top and right-hand panels are window functions.

In the end, KPD 1930 is a star that incorporates a little bit of everything, many pulsation frequencies, multiplets, indications of a tidally induced pulsation geometry, non-sphericity, relativistic Doppler effects, amplitude variations and ellipsoidal variations, all wrapped up in a likely pre-Type Ia supernova binary. Unfortunately, all these effects complicate the analysis, making it a bit of an unruly mess. While we have tried to unravel it, our results indicate that even the WET fails to fully resolve the complexity of the pulsation spectrum and we can only imagine that perhaps Microvariability and Oscillations of Stars or Kepler-like data⁵ would be required to

improve this situation. Unfortunately, the Kepler field just misses KPD 1930. KPD 1930 remains a fascinating star that warrants further attempts to understand its complexities.

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⁵ For information, see <http://www.astro.ubc.ca/MOST/> and <http://astro.phys.au.dk/KASC/>

Table 10. Pulsation frequencies that have an orbital dependence. o− and o+ indicate frequencies detected an orbital alias away while d+ indicates a frequency a daily alias away.

ID	Freq.	QI	QII	QIII	QIV
<i>o1</i>	3787			X	
<i>o2</i>	3799			X	
<i>o3</i>	3831	X			
<i>o4</i> (<i>f16</i>)	3865		X		o−
<i>o5</i>	3882			X	
<i>o6</i> (<i>f23</i>)	3963		d+		X
<i>o7</i>	4008	X			
<i>o8</i>	4031		X	o−	X

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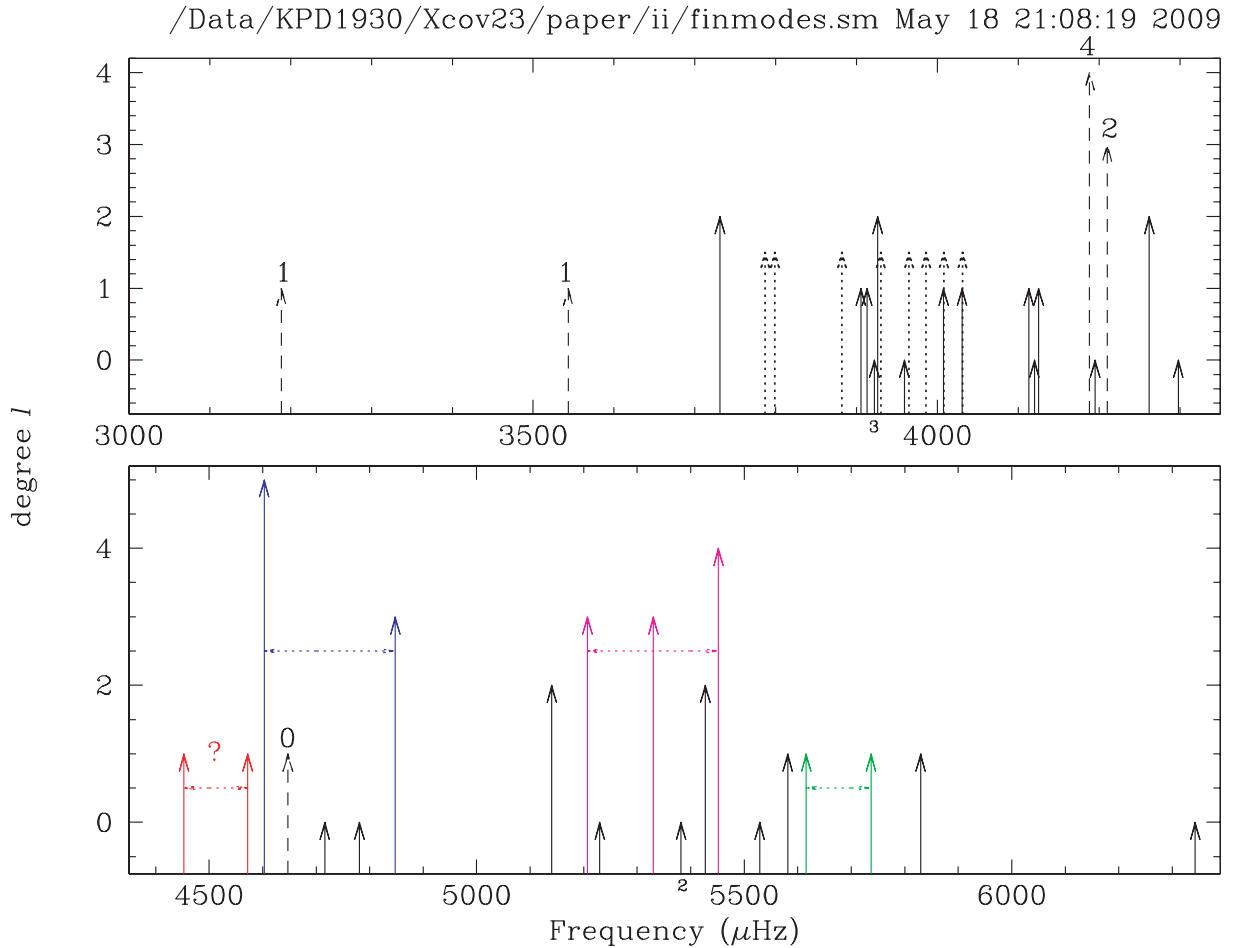


Figure 12. Schematic of modes for KPD 1930. The modal degree (ℓ) is indicated by the height of the arrow. Solid lines indicate the $m = 0$ component of classically interpreted multiplets. For those multiplets with more than one possible $m = 0$ frequency, they are connected by a dotted horizontal line. (They are also colour-coded in the electronic version.) The dashed lines indicate tipped-axis modes, with the m index above the arrow, and the dotted lines indicate frequencies which show a dependence on the orbital phase (set to an arbitrary amplitude of 1.5, as no degree was ascertained for these frequencies).

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SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article:

Figure S1. Detailed pre-whitening sequence of Group IV data between 3600 and 4250 μHz .

Figure S2. Schematic of frequency spacings commensurate with the orbital frequency.

Figure S3. Schematic associating pulsation frequencies with modes for traditionally interpreted multiplets.

Figure S4. Schematic associating pulsation frequencies with possible tipped modes.

Figure S5. Pulsation spectra of Group II's data, separated into opposing phases appropriate for $\ell, m = 1, 0$ and $1, 1$ tipped pulsation axis modes.

Table S1. Pulsation phases and amplitudes for frequencies separated by $>30 \mu\text{Hz}$ for individual runs, daily combined runs and groups of data.

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